

Gravitational-Wave Data Analysis

Peter Shawhan



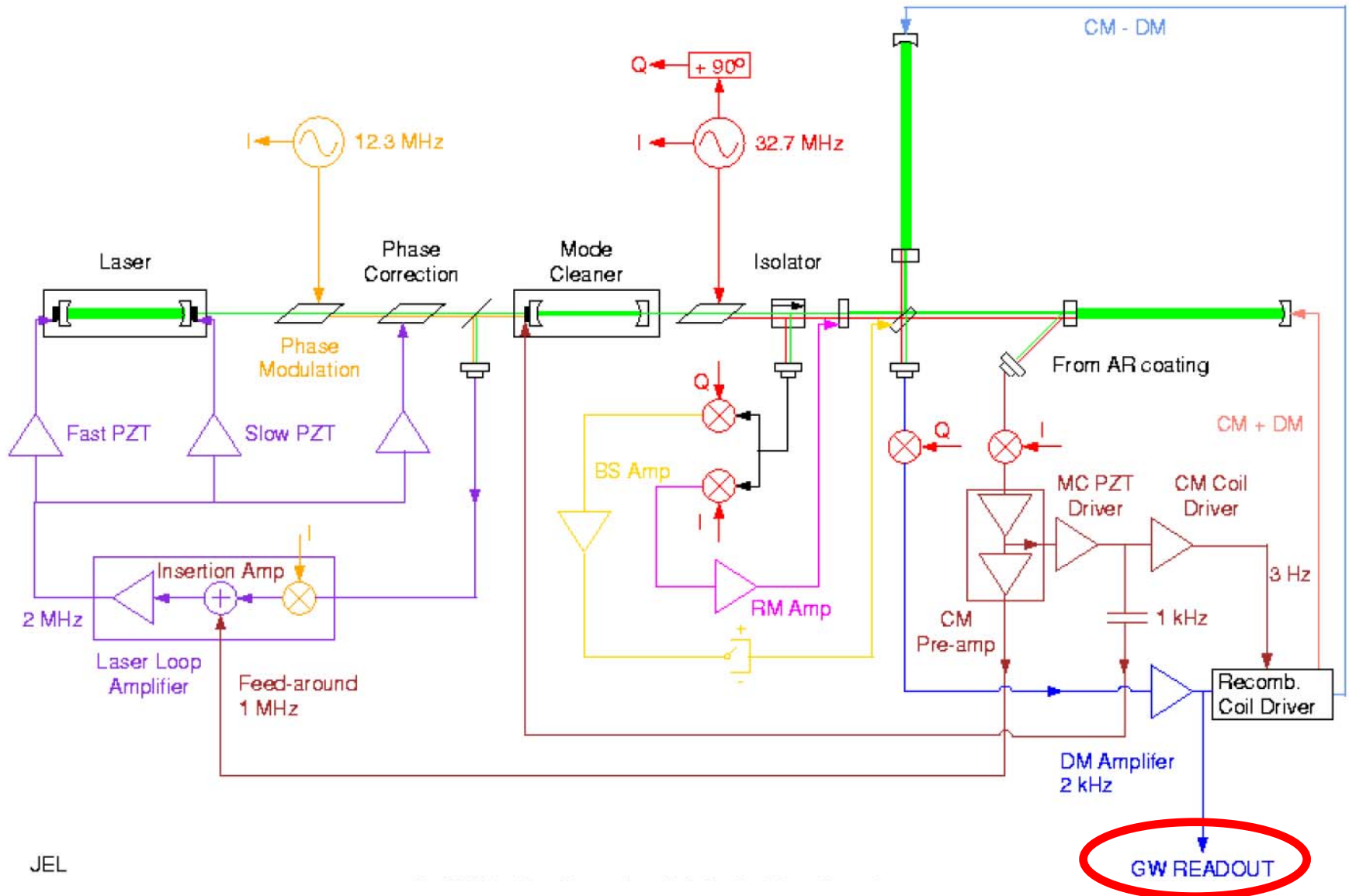
Physics 798G
April 12, 2007



Outline

- ▶ **Gravitational-wave data**
- ▶ **General data analysis principles**
- ▶ **Specific data analysis methods**
 - ▶ Classification of signals
 - ▶ Methods for each class of signals
- ▶ **Idiosyncracies of real detectors**
- ▶ **The gravitational-wave community**

Length Sensing and Control





Gravitational-Wave Data

Instantaneous estimate of strain for each moment in time

i.e. demodulated channel sensitive to arm length difference

(Or, for resonant detector: displacement sensed by transducer)

Digitized time series recorded in computer files

LIGO / GEO sampling rate: 16384 Hz

VIRGO sampling rate: 20000 Hz

Synchronized with GPS time

Common “frame” file format (*.gwf)

***Many* auxiliary channels recorded too**

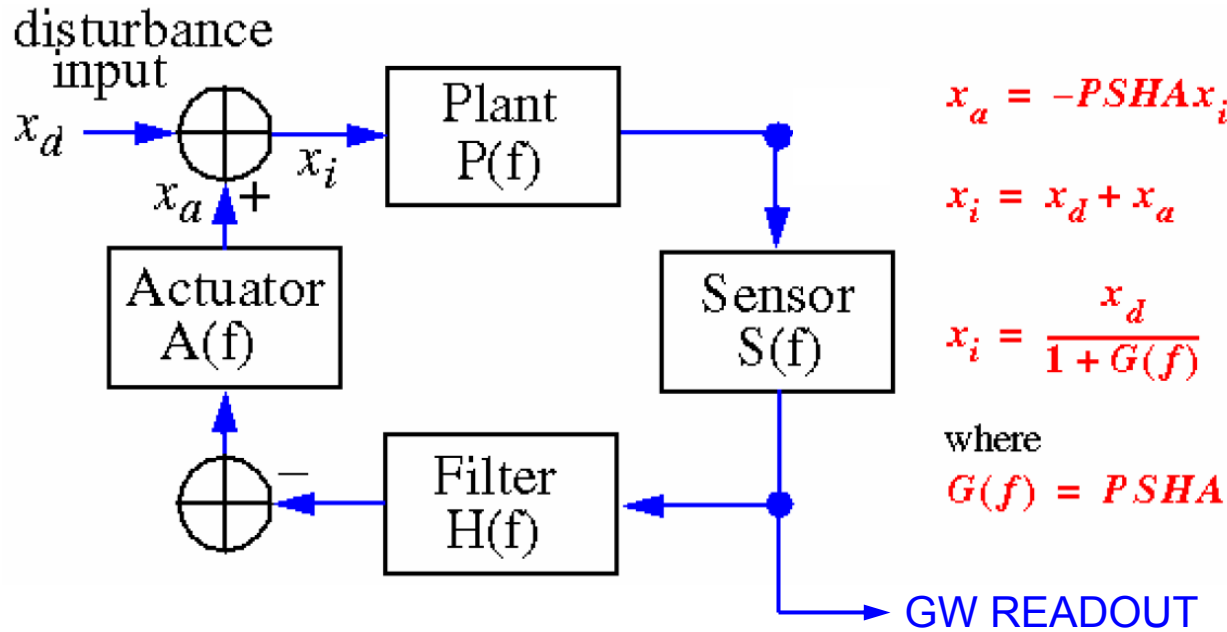
Interferometric sensing and control

Environmental sensors (accelerometers, microphones, magnetometers,...)

Interferometer configuration and facilities housekeeping data

Total data volume: a few megabytes per second per interferometer

Calibration



Monitor P(f) continuously with “calibration lines”

Sinusoidal arm length variations with known absolute amplitude

Apply frequency-dependent correction factor to get GW strain

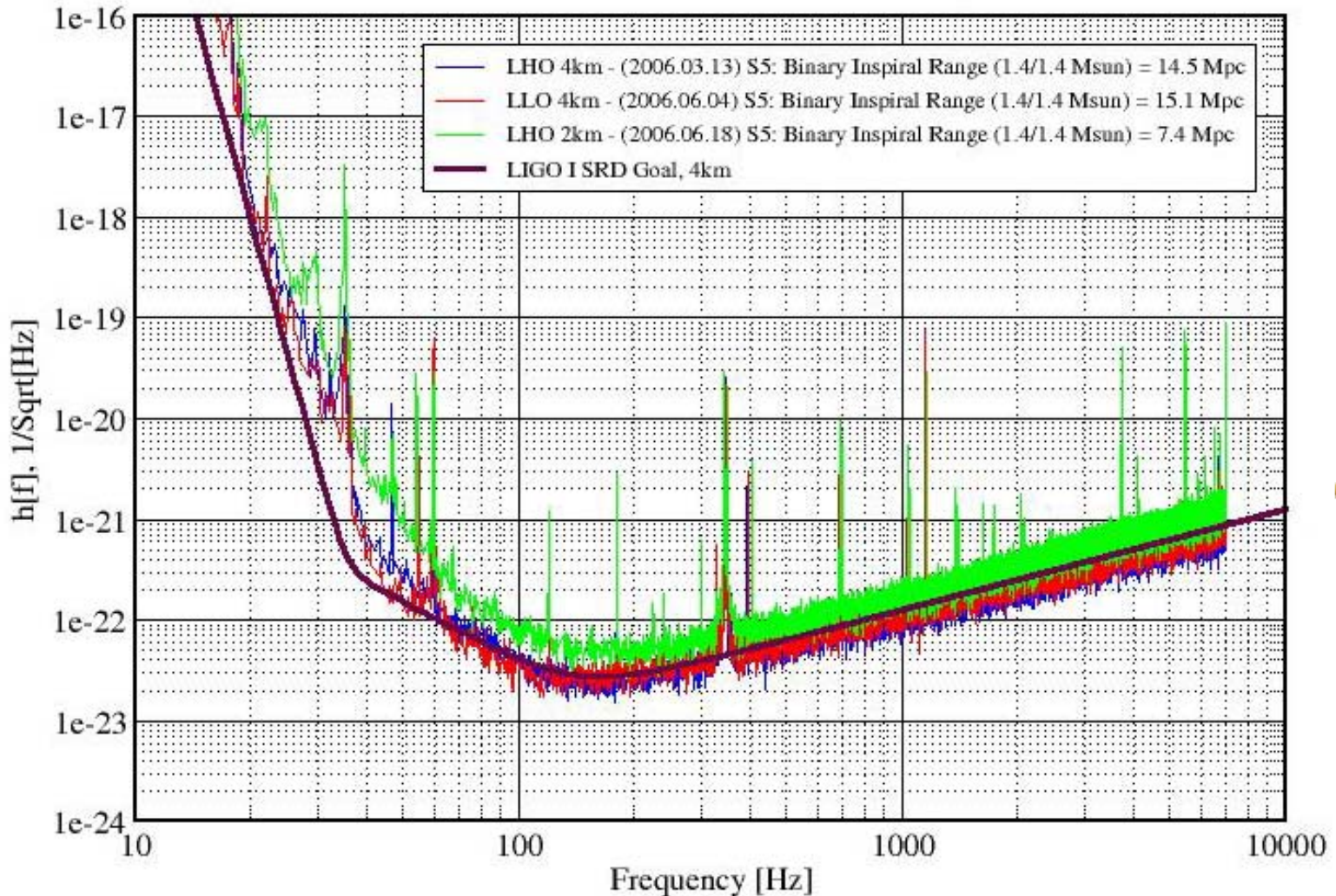
$$h = (\text{GW READOUT}) \times \frac{1 + G(f)}{P(f) S(f)}$$



Gravitational-Wave Strain Data

Strain Sensitivity for the LIGO 4km Interferometers

S5 Performance - June 2006 LIGO-G060293-01-Z





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Basic Principles

Gravitational wave sources are rare and/or intrinsically weak

Need highly sensitive detectors

A detectable signal will most likely be near threshold of detectability

Claiming the first detection will be a big deal

Past detection claims failed to be confirmed

Want to set a high standard of evidence

Require consistency among multiple detectors

Individual detectors may glitch

Require coincidence or cross-coherence of some sort

Allow for relative time delay, different antenna response, sensitivities

Estimate false alarm rate (“background”) using time-shifted data

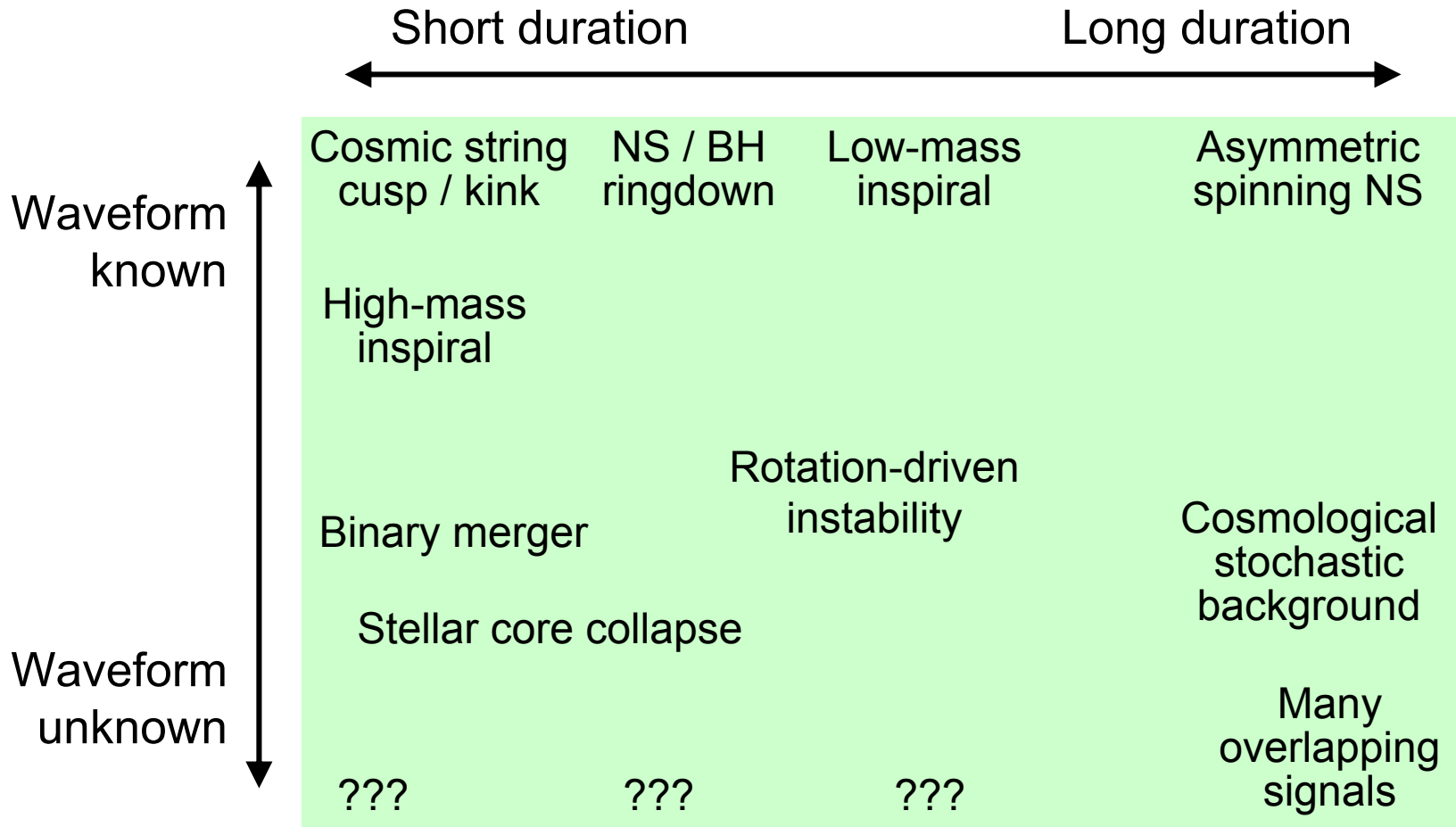


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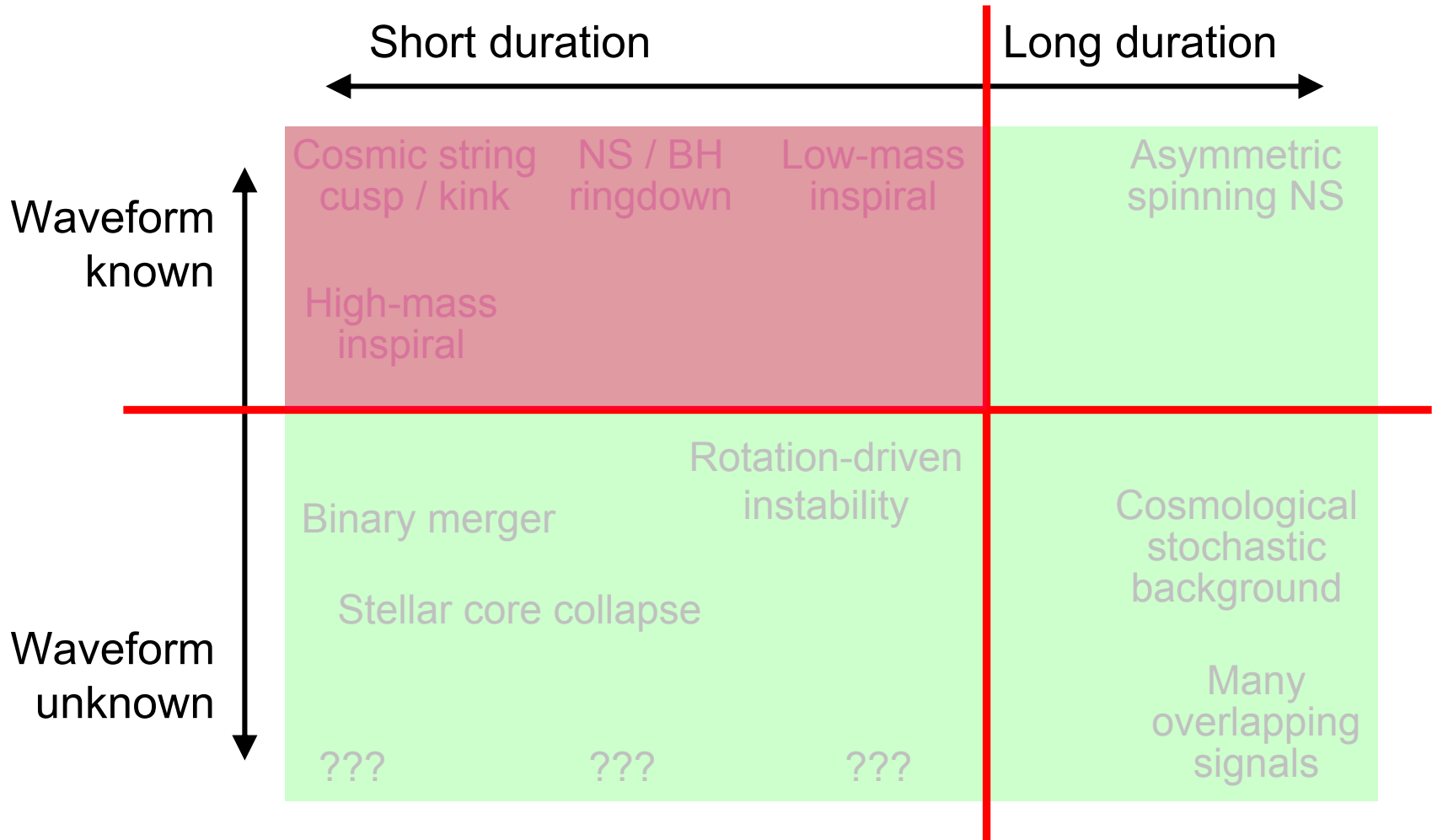


The Gravitational Wave Signal Tableau



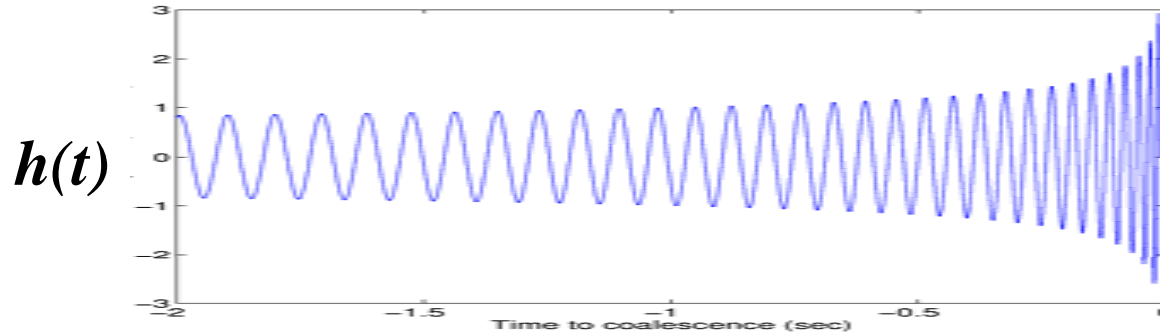


Signal Classes





Short-duration, Known Waveforms: Inspirals, etc.



Known well, or fairly well, in some parametrized space

e.g. post-Newtonian expansion (assumes negligible spins)

$$\Psi(f) = 2\pi f t_c + \frac{3}{128\eta} (\pi m f)^{-5/3}$$

$$+ \frac{5}{96\eta} \left(\frac{743}{336} + \frac{11}{4}\eta \right) (\pi m f)^{-1} \quad \text{1PN}$$

$$- \frac{3\pi}{8\eta} (\pi m f)^{-2/3} \quad \text{1.5PN}$$

$$+ \frac{15}{64\eta} \left(\frac{3058673}{1016064} + \frac{5429}{1008}\eta + \frac{617}{144}\eta^2 \right) (\pi m f)^{-1/3} \quad \text{2PN}$$

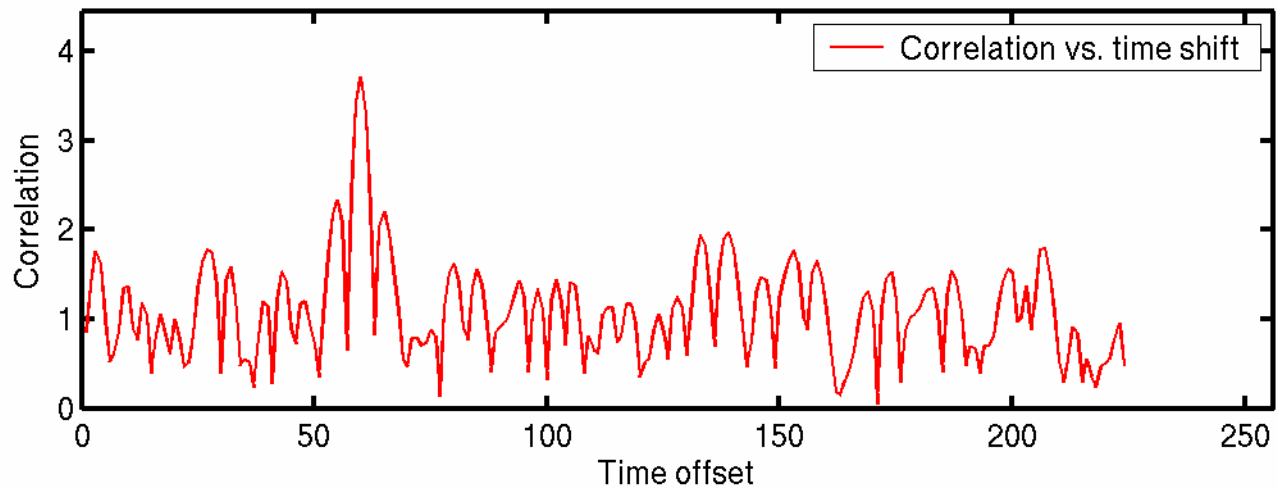
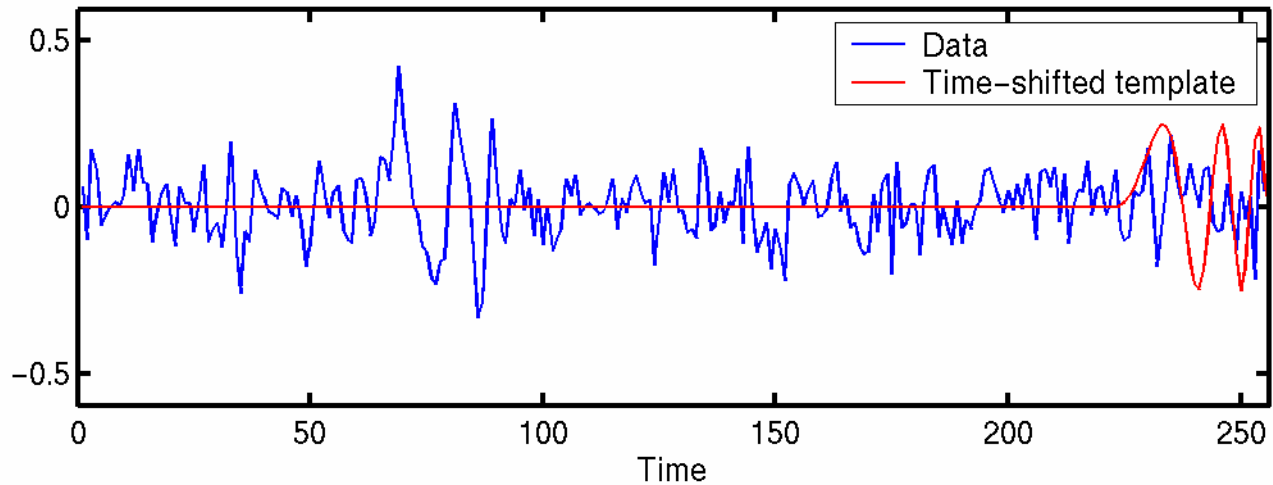
+ ...

where $m = (m_1 + m_2)$, $\eta = \frac{m_1 m_2}{m^2}$

**Known waveform \Rightarrow
Use **matched filtering****



Basic Matched Filtering





Source Parameters vs. Signal Parameters

Inspiral source parameters

Masses (m_1, m_2)

Spins

→ Assume negligible for now

Orbital phase at coalescence

→ Maximize analytically when filtering

Inclination of orbital plane

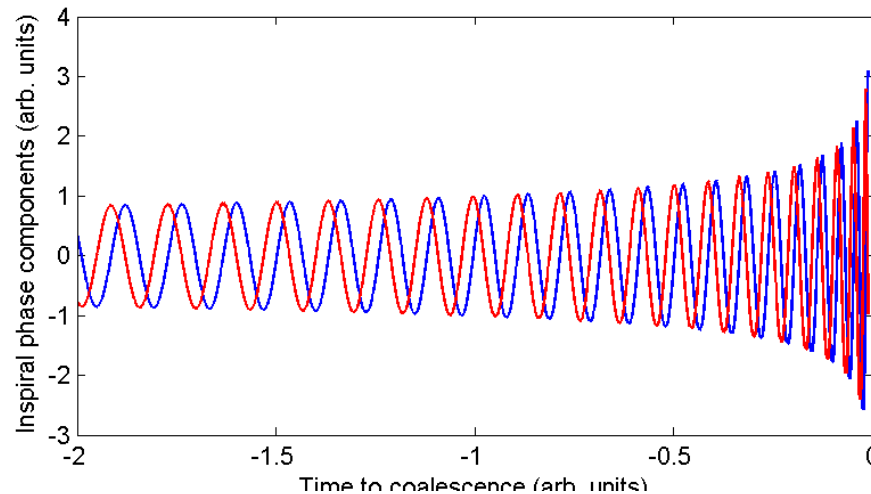
Sky location

→ Simply multiplicative for a given detector

Distance

→ Simply multiplicative

Filter with orthogonal templates, take quadrature sum





Optimal Matched Filtering in Frequency Domain

Data after FFT

Template, generated in freq. domain using stationary phase approx.

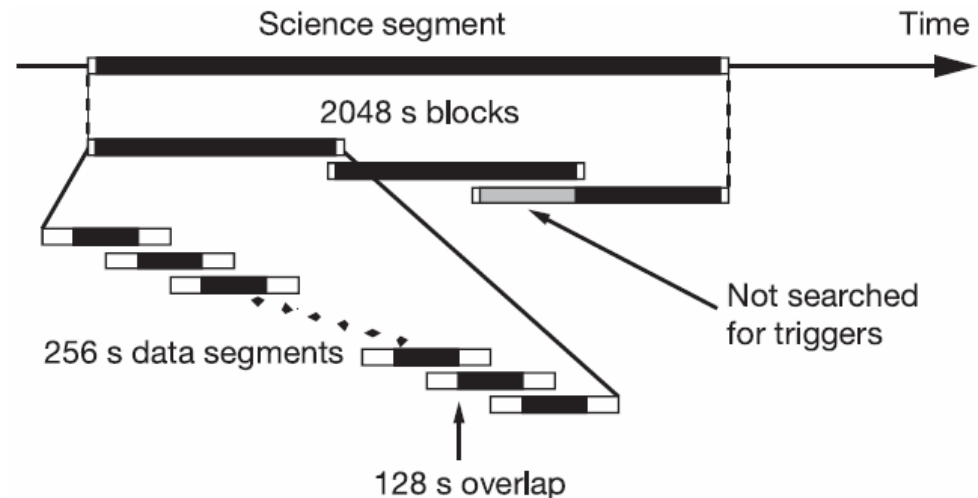
$$z(t) = 4 \int_0^{\infty} \frac{\tilde{s}(f) \tilde{h}^*(f)}{S_n(f)} e^{2\pi i f t} df$$

Noise power spectral density

Look for maximum of $|z(t)|$ above some threshold \rightarrow **trigger**

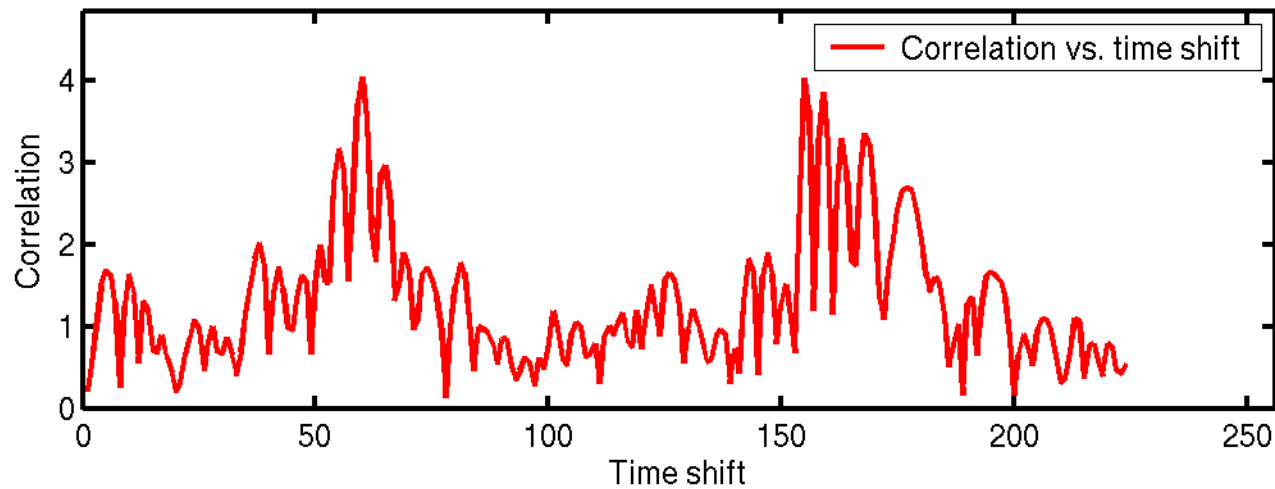
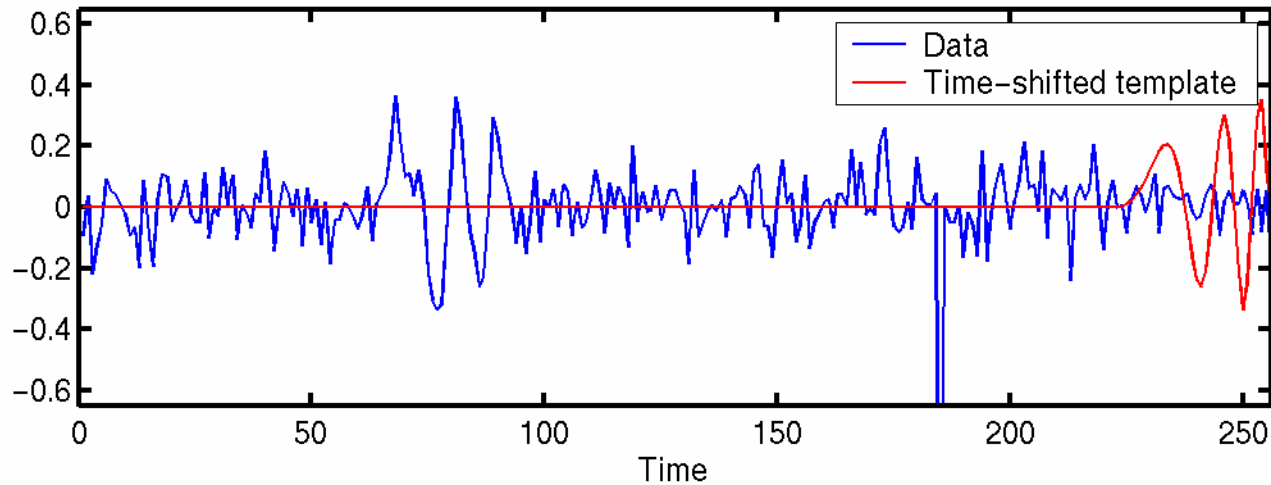
Search overlapping intervals to cover science segment, avoid wrap-around effects

Estimate power spectrum from bin-by-bin median of fifteen 256-sec data segments





Matched Filtering Susceptibility to Glitches

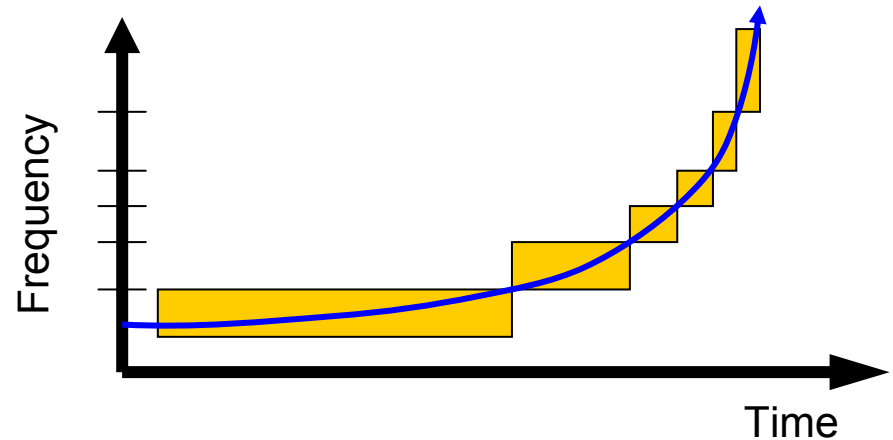


Waveform Consistency Tests

Chi-squared test

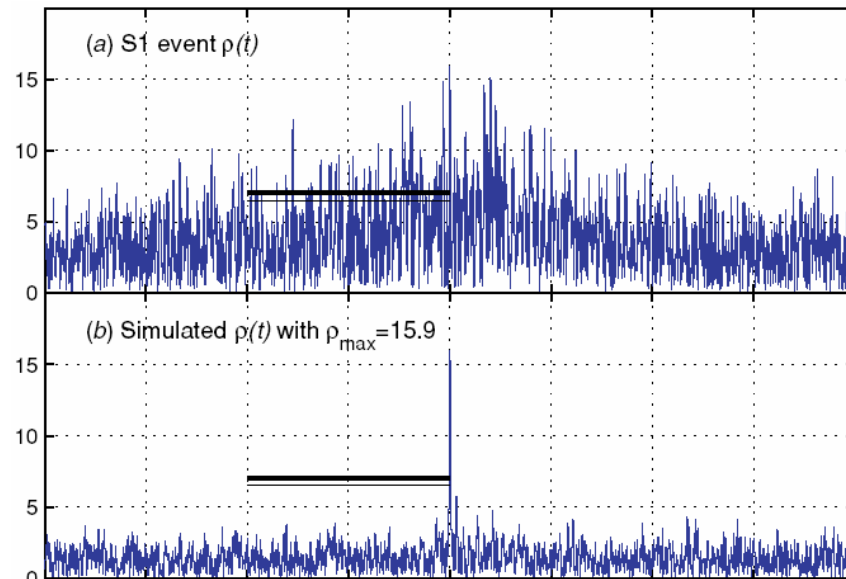
Divide template into p parts,
calculate

$$\chi^2(t) = p \sum_{l=1}^p \left\| z_l(t) - z(t)/p \right\|^2$$



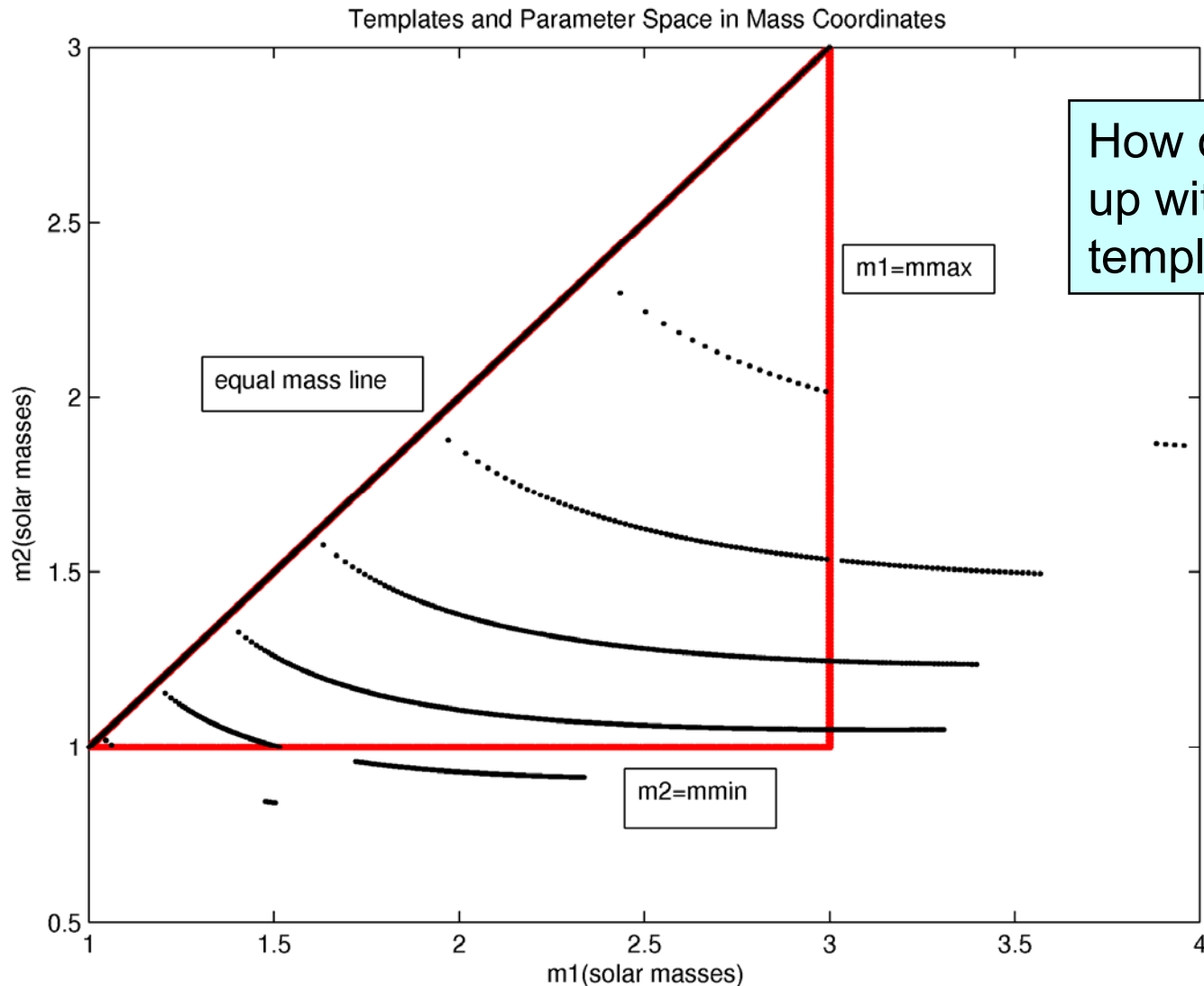
Tests using filter output

e.g. time above threshold





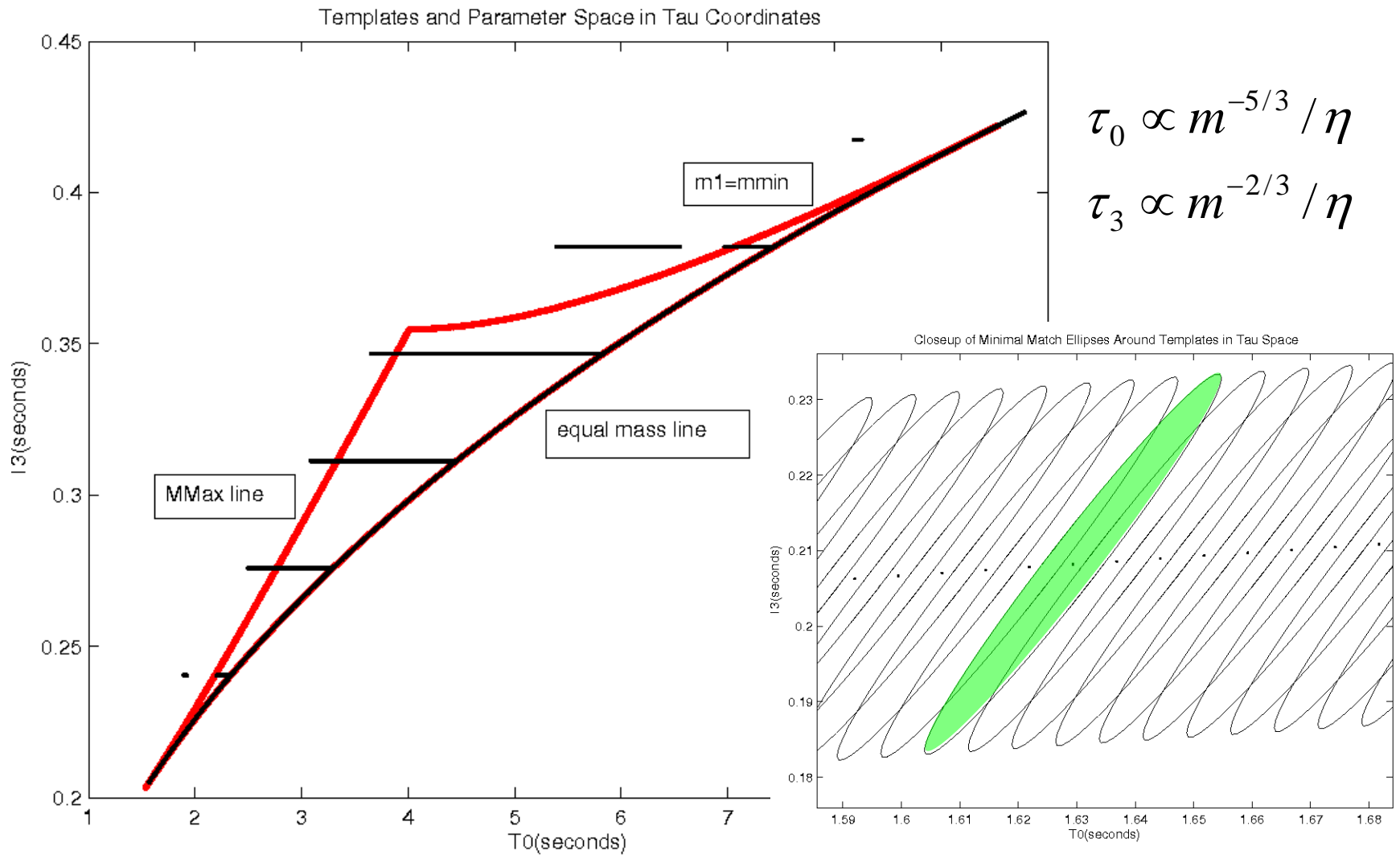
Template Bank Construction



How did we come up with this set of templates???

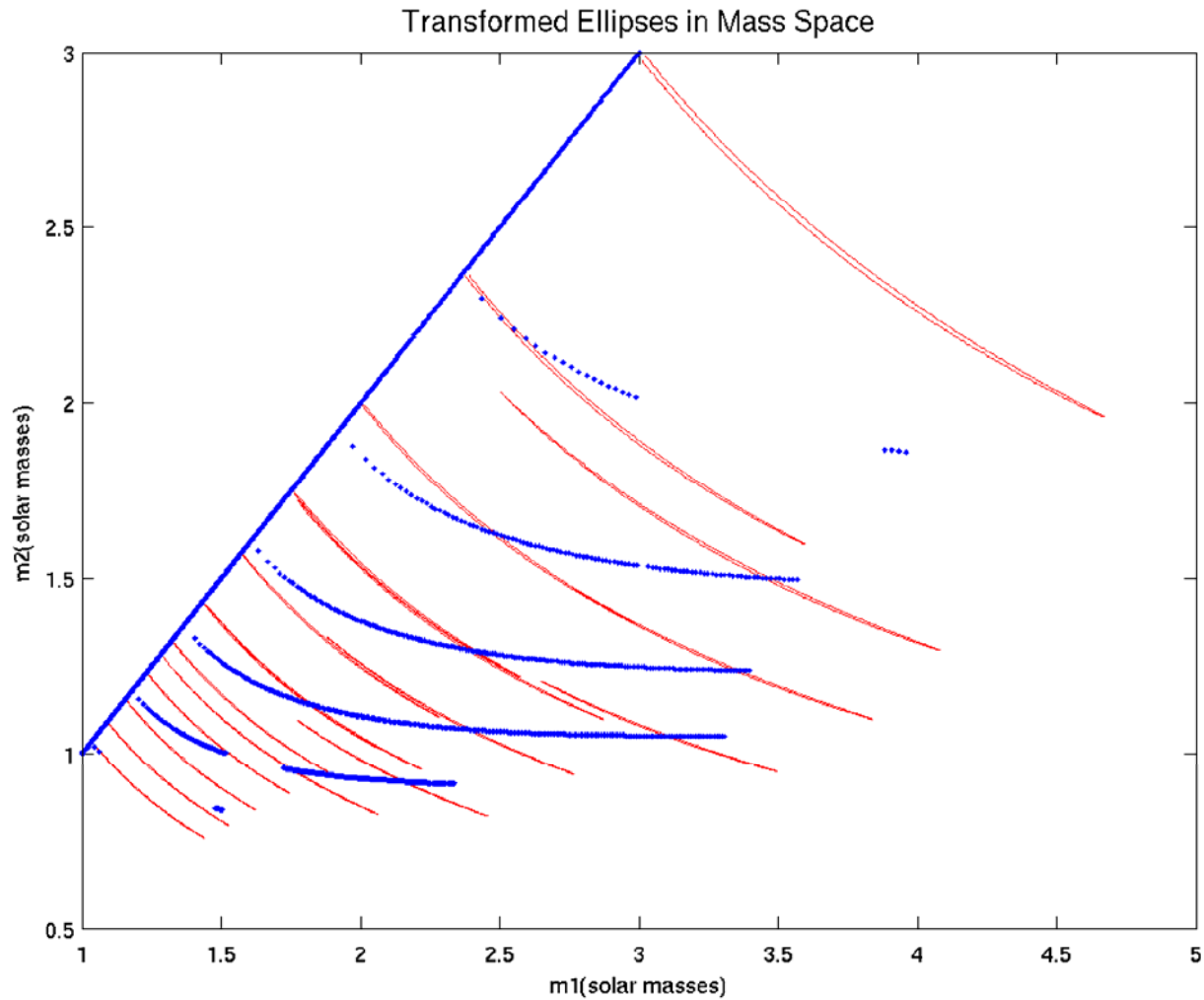


Template Bank Construction in (τ_0, τ_3) space



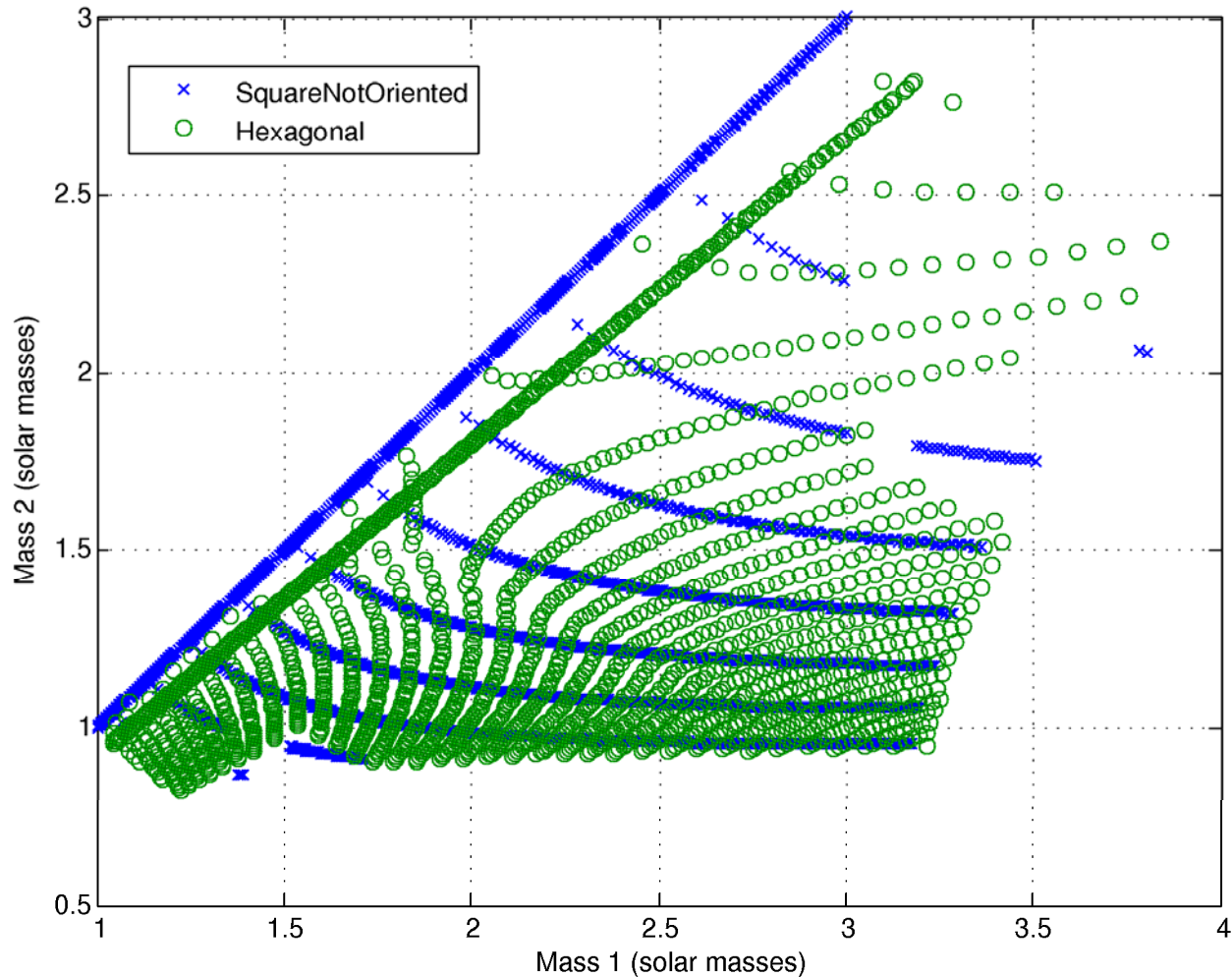


Ellipses in Mass Space





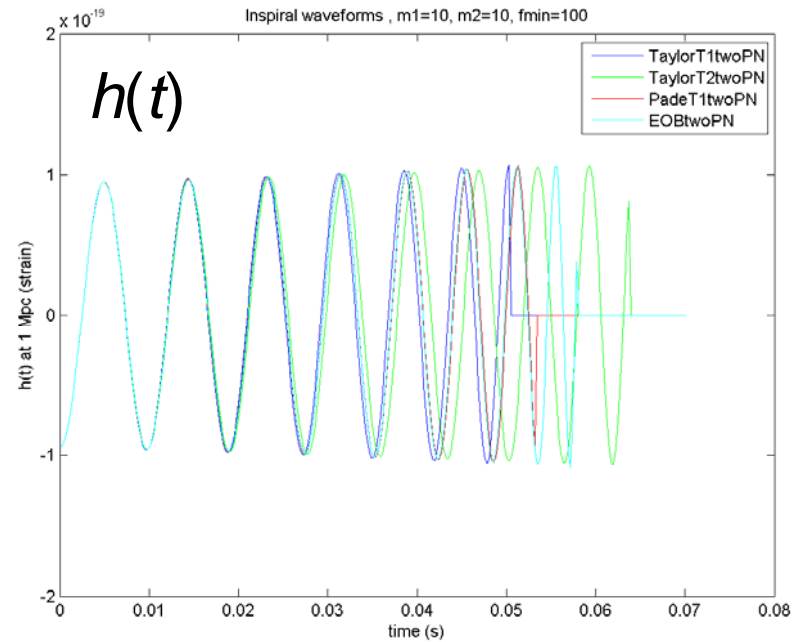
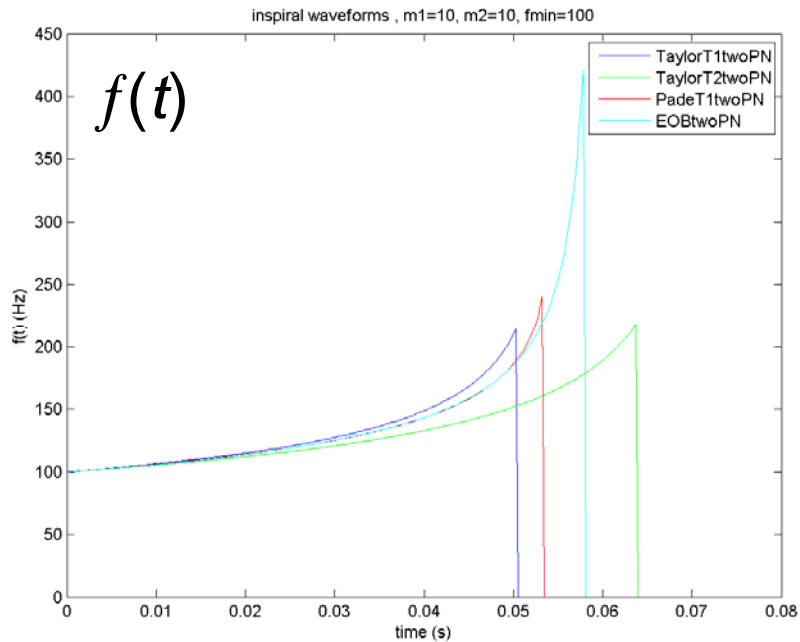
Different Bank Layout Methods





Uncertain Waveforms for High-Mass Inspirals

Different models for $10+10 M_{\text{sun}}$ black hole binary inspiral





Templates for Detection vs. Parameter Estimation

Can use a parametrized space of templates

e.g. Buonanno, Chen, and Vallisneri, Phys. Rev. D 67, 104025 (2003)

$$h(f) = f^{-7/6} (1 - \alpha f^{2/3}) \theta(f_{cut} - f) \exp[i(\phi_0 + 2\pi t_0 f + \psi_0 f^{-5/3} + \psi_3 f^{-2/3})]$$

Analytically calculate α to maximize SNR

Parameters of the search

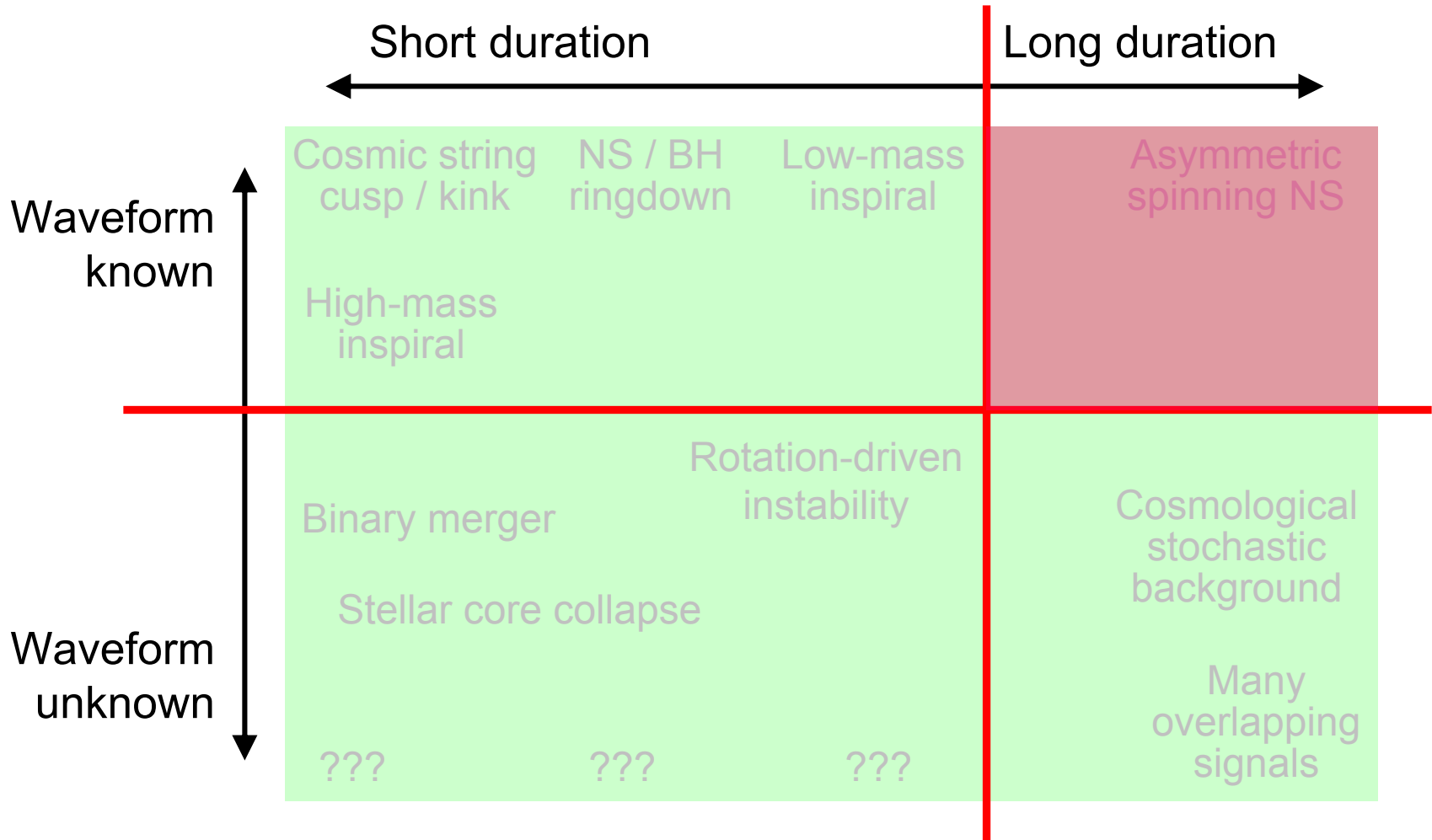
This can match the various waveform models rather well

Intended for binary components with negligible spin

Once a signal is detected, re-filter with physical templates to extract physical parameters



Signal Classes



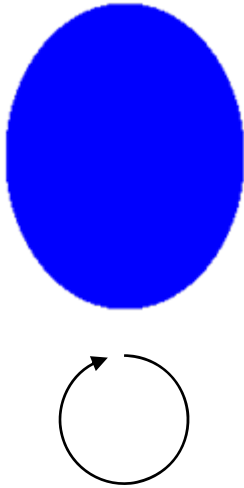


Continuous, Known Waveform: GW from Spinning Neutron Stars

If not axisymmetric, will emit gravitational waves

Example: ellipsoid with distinct transverse axes

Along spin axis:



From side:





Continuous GW Signals at Earth

Start with a sinusoidal signal with spin-down term(s)

Polarization content depends on orientation/inclination of spin axis

Amplitude modulation

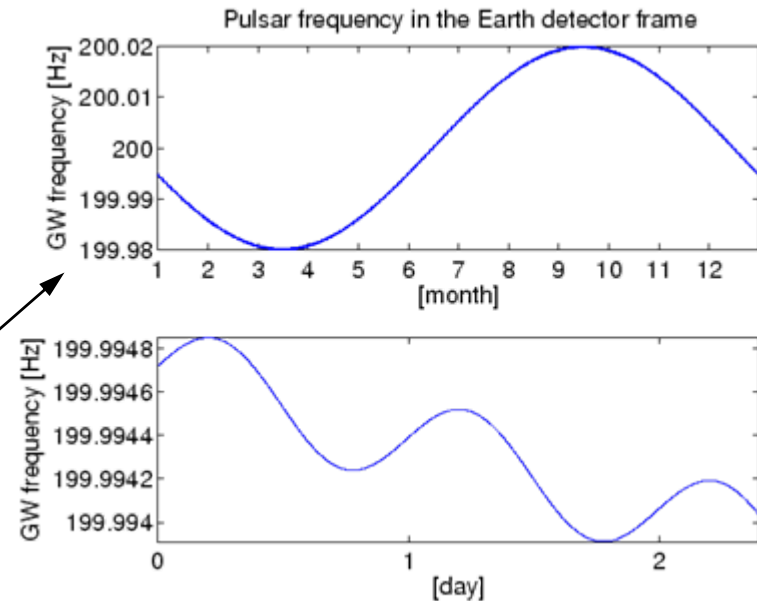
Polarization projection changes over a sidereal day

Doppler shift

$$\frac{\Delta f}{f} = \frac{\mathbf{v} \cdot \mathbf{n}}{c}$$

Annual variation: up to $\sim 10^{-4}$

Daily variation: up to $\sim 10^{-6}$



GW signals from binary systems are more complicated !

Additional Doppler shift due to orbital motion of neutron star

Varying gravitational redshift if orbit is elliptical

Shapiro time delay if GW passes near companion



Search Methods for CW signals

Several cases to consider:

- Sky position and spin frequency known accurately
- Sky position and spin frequency known fairly well
- Sky position known, but frequency and/or binary orbit parameters unknown
- Search for unknown sources in favored sky regions

- Search for unknown sources over the whole sky

Candidates

Radio pulsars

X-ray pulsars

LMXBs

Globular clusters

Galactic center

Supernova remnants

Unseen isolated
neutron stars

Different computational challenges \Rightarrow Different approaches



Search for Gravitational Waves from Known Pulsars

Method: heterodyne time-domain data using the known spin phase of the pulsar

Requires precise timing data from radio or X-ray observations

Include binary systems in search when orbits known accurately

Exclude pulsars with significant timing uncertainties

Special treatment for the Crab and other pulsars with glitches, timing noise



Wide Parameter Space Searches

Method: matched filtering with a bank of templates

Parameters:

Sky position

Spin axis inclination and azimuthal angle

Frequency, spindown, initial phase

Binary orbit parameters (if in a binary system)

Use a detection statistic, \mathcal{F} , which analytically maximizes over spin axis inclination & azimuthal angle and initial phase

Even so, computing cost scales as $\sim T^6$

Detection threshold also must increase with number of templates

Check for signal consistency in multiple detectors

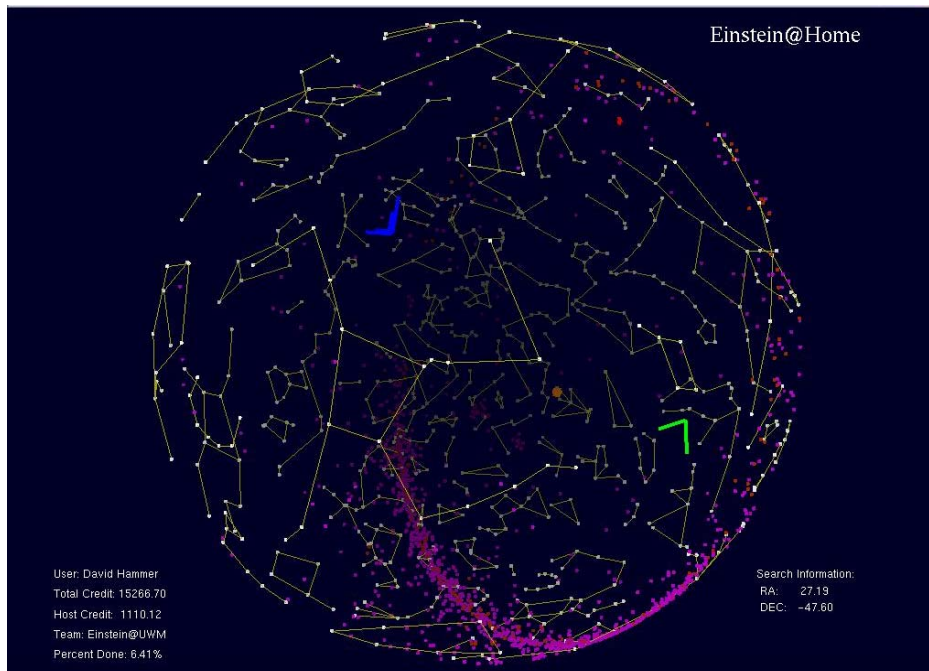
Problem: huge number of templates needed



Getting by with a Little Help from Our Friends

Public distributed computing project: [Einstein@Home](#)

Small bits of data distributed for processing; results collected, verified, and post-processed



Screen saver graphics

So far 156,000 users, currently providing ~77 Tflops



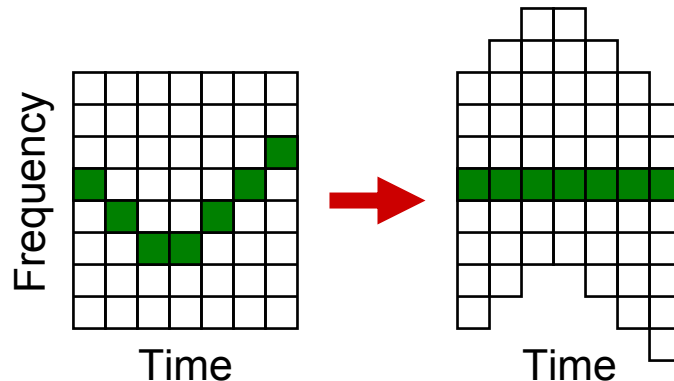
Semi-Coherent Search Methods

Can't do an all-sky coherent search using all of the data

Divide data into time intervals, calculate power, sum it

Less sensitive for a given observation time, but computationally more efficient, so can use **all** the data

Generally use 30-minute “short Fourier transforms” (SFTs)



Different methods of adding SFTs

“StackSlide” : sums normalized power

“PowerFlux” : sums normalized power with weights for sky position, noise

“Hough” : sums binary counts with weights for sky position, noise

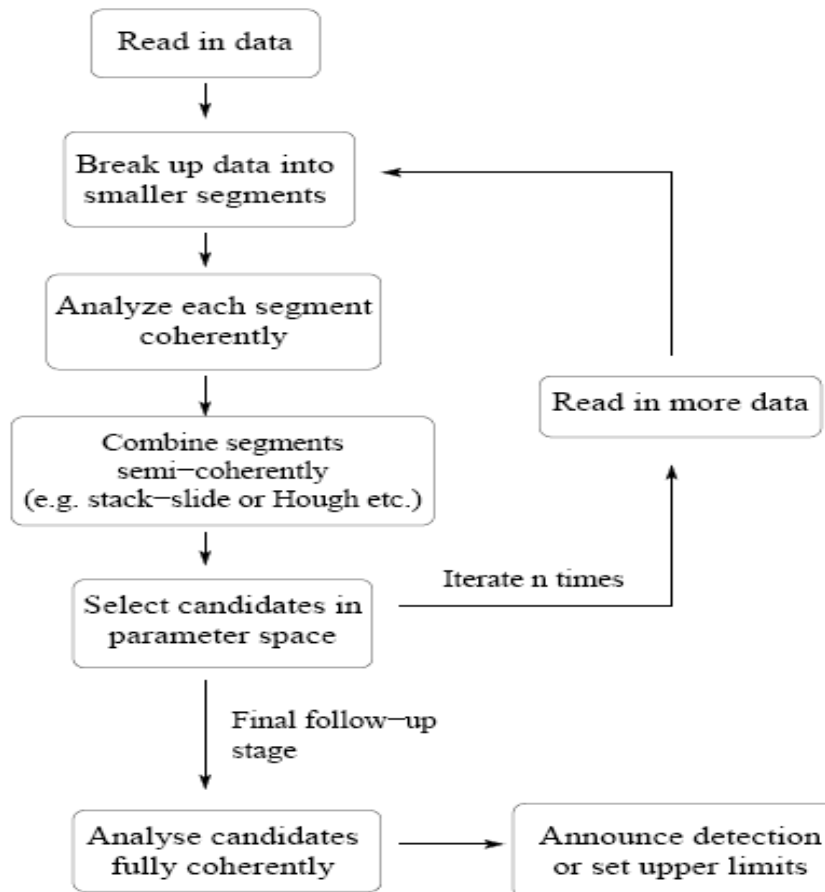


Hierarchical Search

Alternate semi-coherent and fully coherent stages

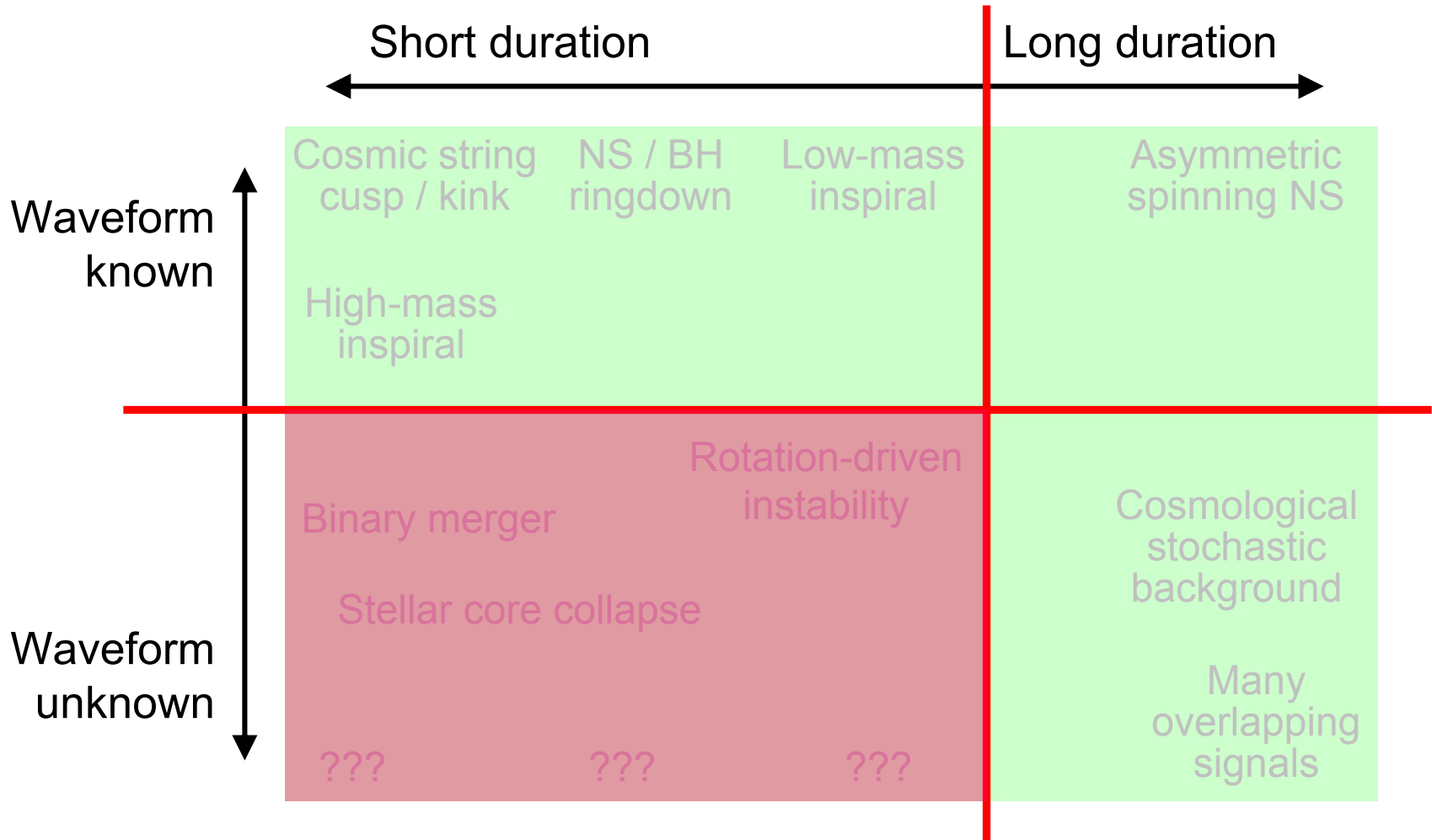
Gets closer to optimal sensitivity, at a manageable CPU cost

Example:





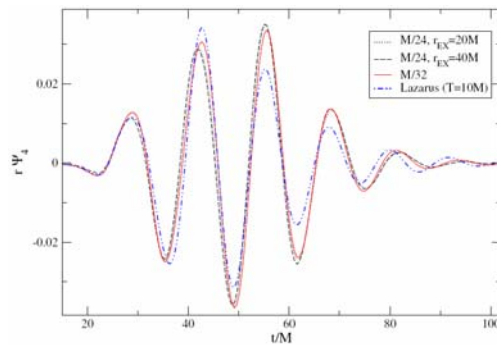
Signal Classes



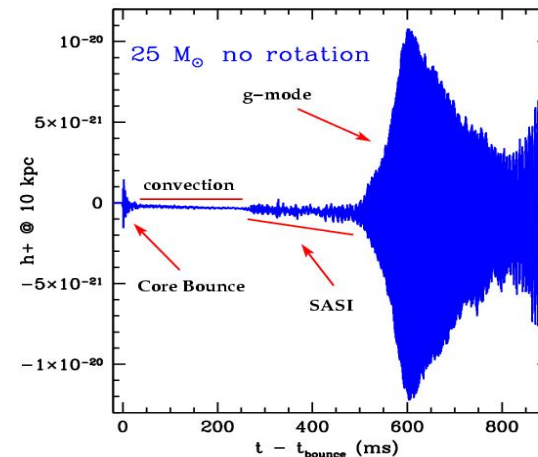
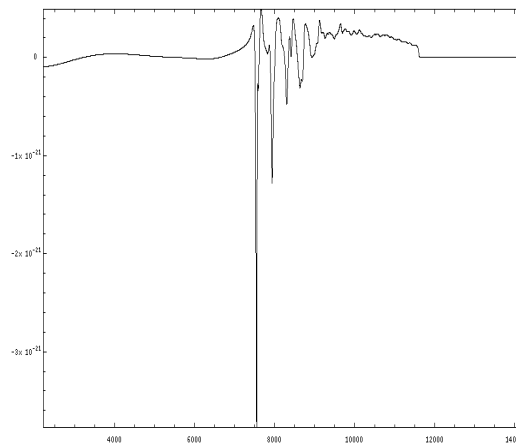
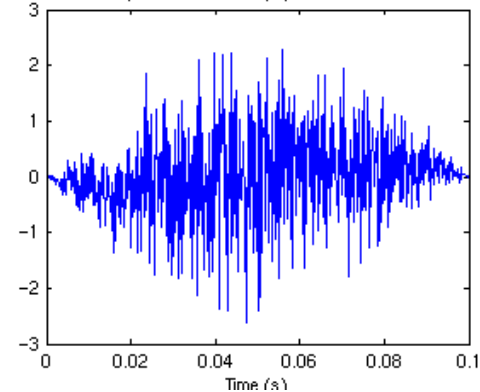
Short-duration, Unknown Waveform: Gravitational-Wave Bursts

We're exploring the sky – Who knows what is out there to find?

Want to be able to detect **any arbitrary signal**



White noise, half-sine envelope, 0.100000 sec duration





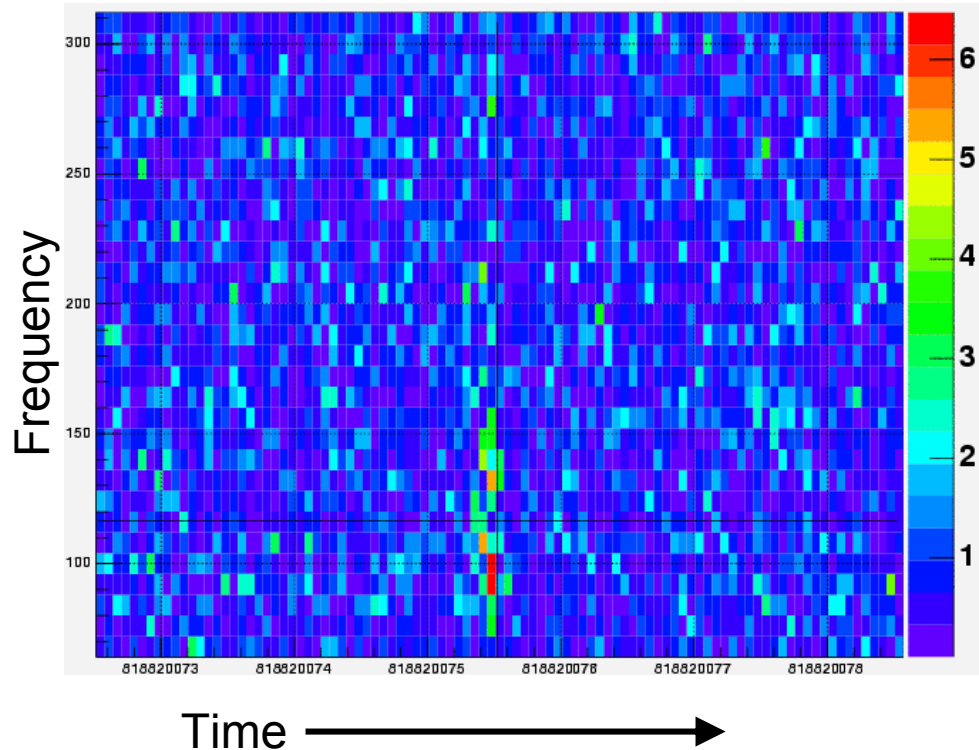
“Excess Power” Search Methods

Decompose data stream into time-frequency pixels

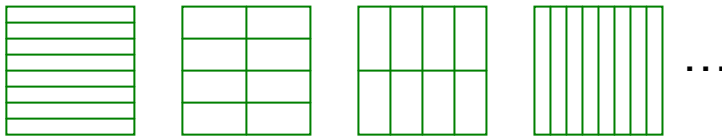
Fourier components, wavelets, “Q transform”, etc.

Normalize relative to noise as a function of frequency
as a function of frequency

Look for “hot” pixels or clusters of pixels

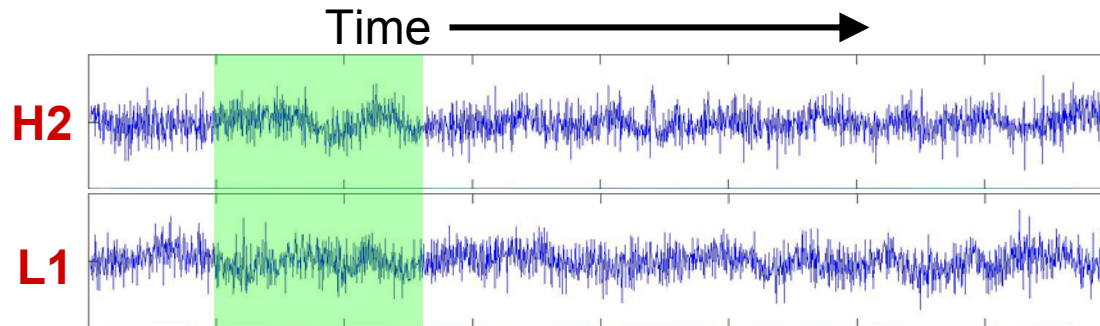


Can use multiple $(\Delta t, \Delta f)$ pixel resolutions



Cross-Correlation Methods

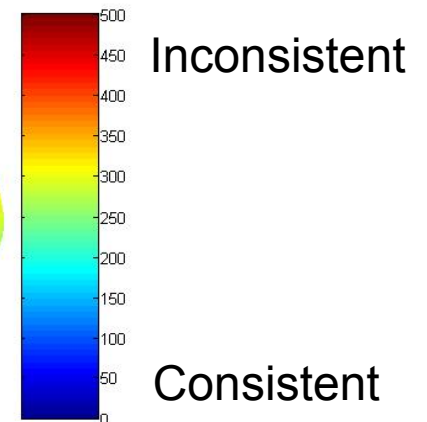
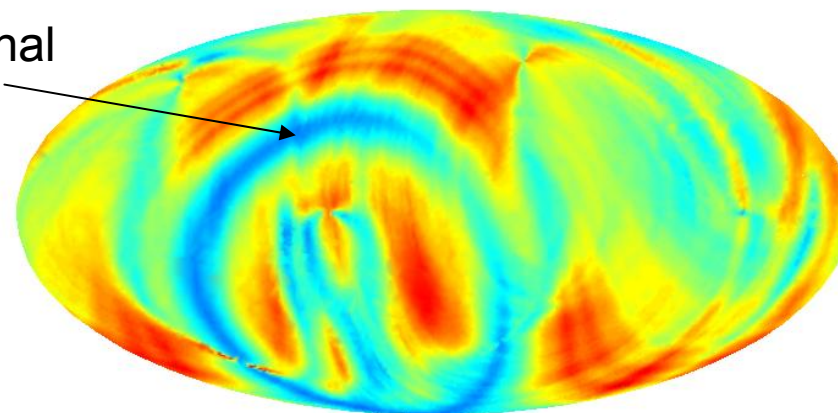
Look for same signal buried in two data streams



Integrate over a time interval comparable to the target signal

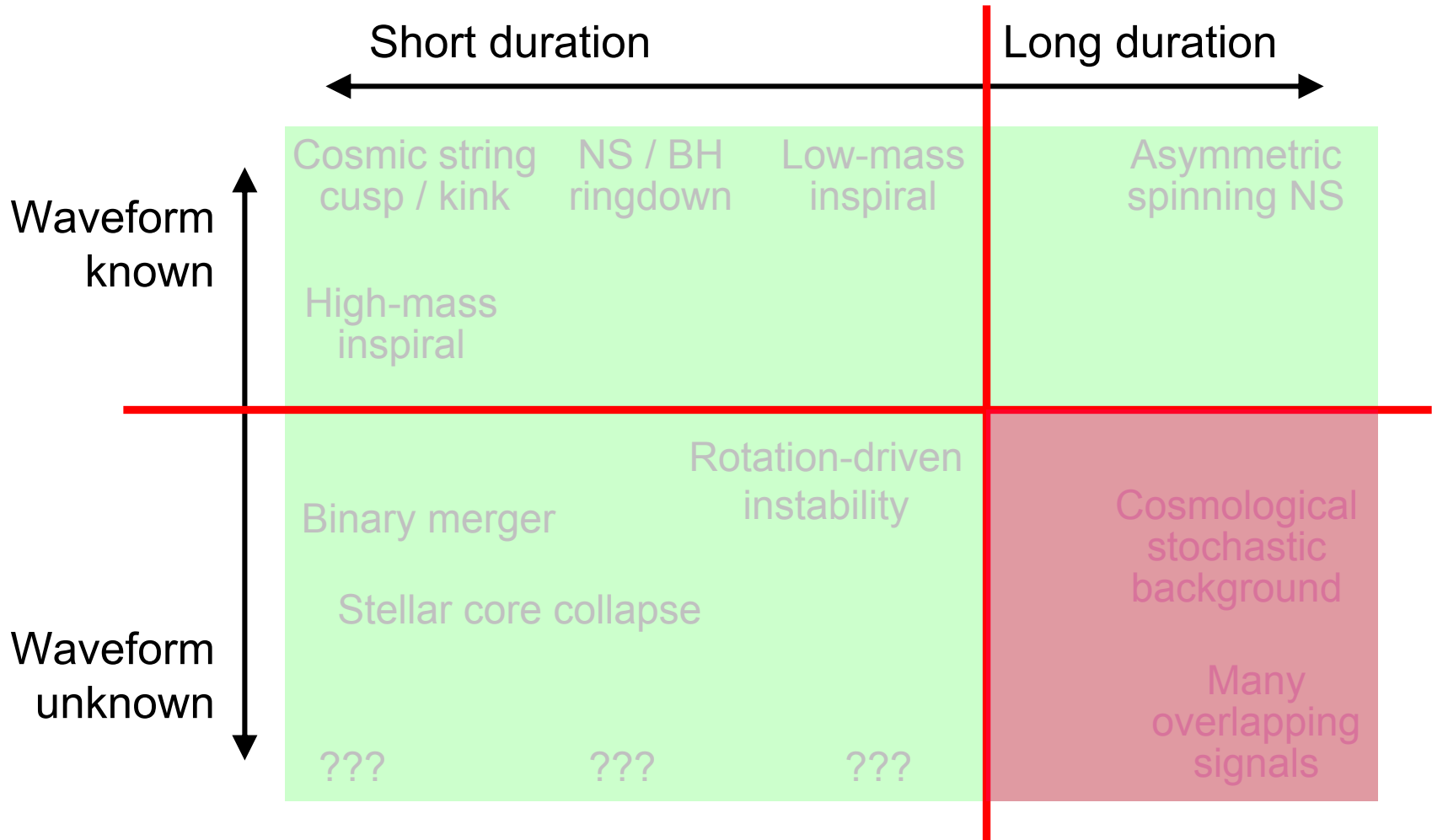
Extensions to three or more detector sites being worked on

Simulated signal injected here





Signal Classes





Continuous, Unknown Waveform: Stochastic Gravitational Waves

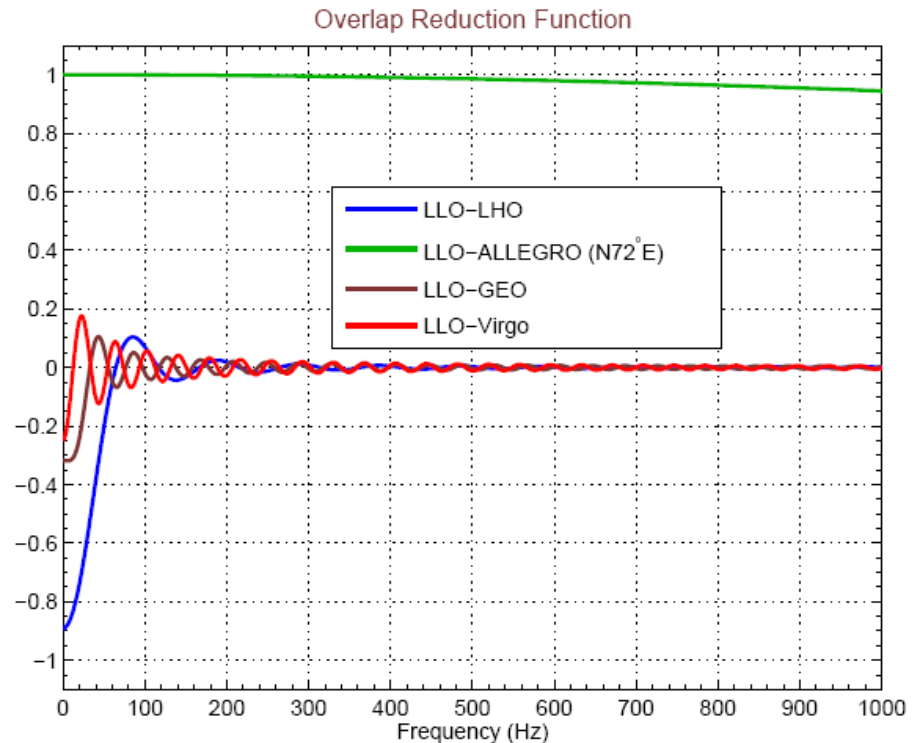
Use **cross-correlation** to search for signal smaller than detector noise

For isotropic stochastic GWs, know what correlation to expect between any given pair of detectors

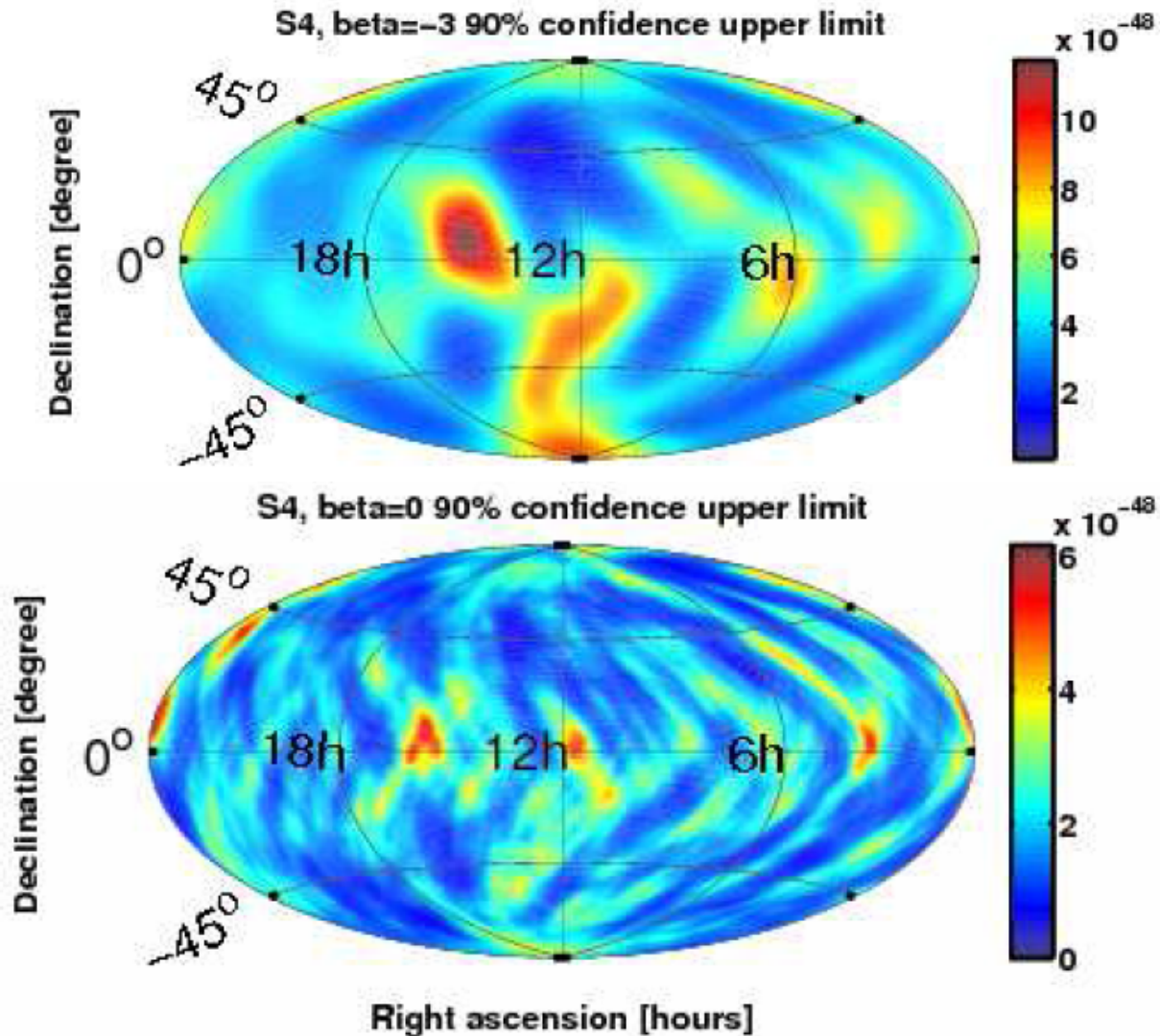
Optimal filter:

$$Y = \int df \tilde{s}_1^*(f) \tilde{Q}(f) \tilde{s}_2(f)$$

$$\tilde{Q}(f) \propto \frac{f^{-3} \Omega_{\text{GW}}(f) \gamma_{12}(f)}{P_1(f) P_2(f)}$$



Sky Map of Stochastic Gravitational Waves: “Radiometer”





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Variable Data Quality

Various environmental and instrumental conditions catalogued;
can study relevance using *time-shifted* coincident triggers

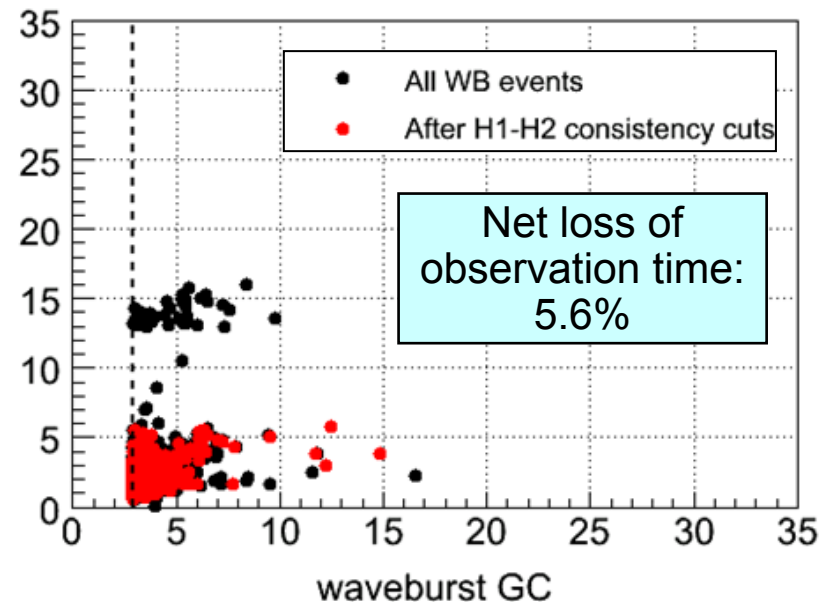
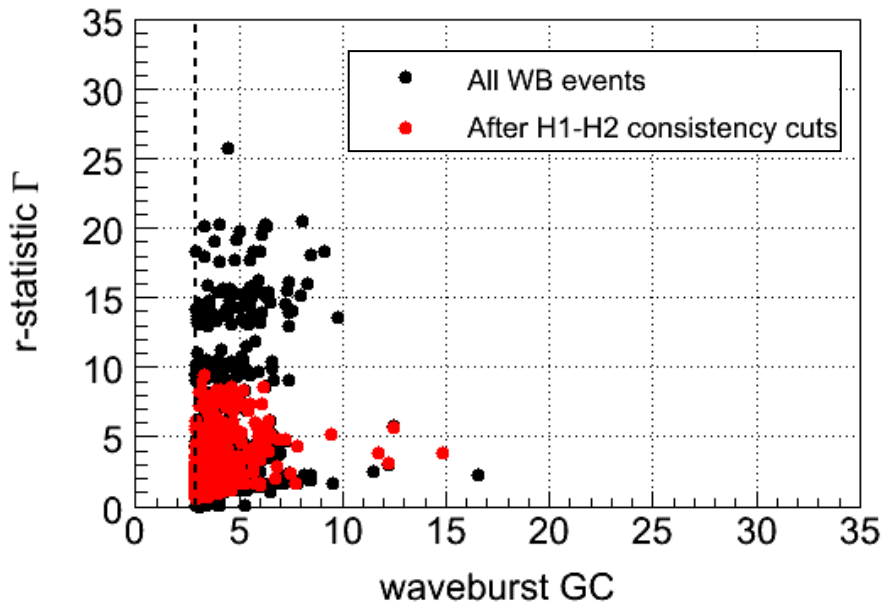
Example from S4 all-sky burst search:

Minimal data quality cuts

- Require locked interferometers
- Omit hardware injections
- Avoid times of ADC overflows

Additional data quality cuts

- Avoid high seismic noise, wind, jet
- Avoid calibration line drop-outs
- Avoid times of “dips” in stored light
- Omit last 30 sec of each lock

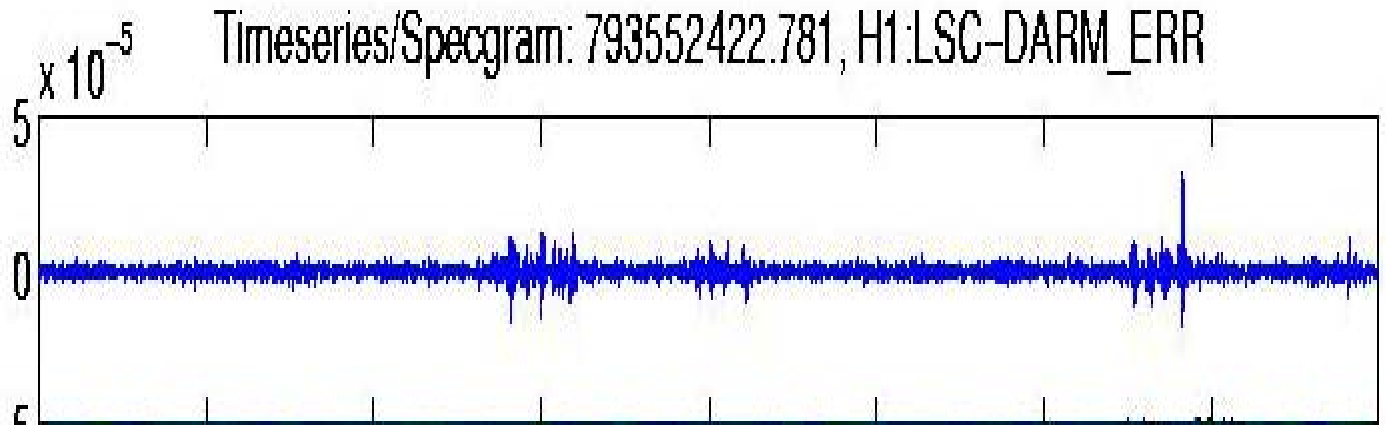




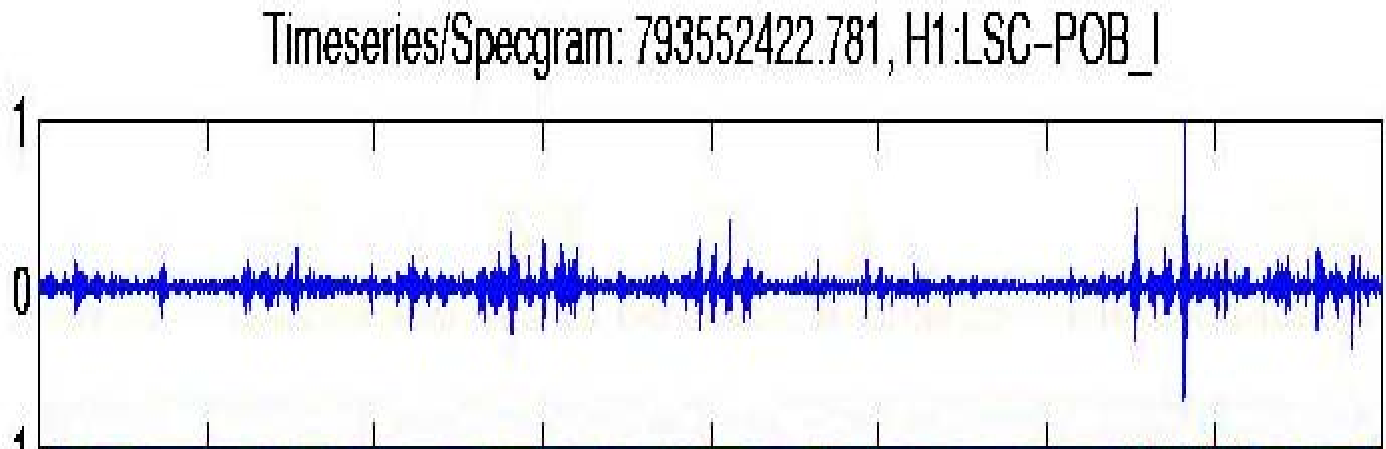
Non-Stationary Noise / Glitches

Auxiliary-channel vetoes

GW
channel



Beam
splitter
pick-off





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Big Science!

The LIGO Scientific Collaboration

A few hundred people from ~50 institutions

Includes everyone from GEO

LIGO and GEO data analyzed together

Virgo

TAMA 300

Bar detectors (ALLEGRO, AURIGA, EXPLORER, NAUTILUS)

Cooperative observing and joint data analysis

LIGO and TAMA 300, LIGO and ALLEGRO, LIGO and AURIGA,
VIRGO and Explorer+Nautilus

LIGO-VIRGO data exchange and joint analysis begins May 18