

11-12:15 ← not much time!

Beyond GR

1811  
-1877

~~gravity at long distances~~

Intro: GR { theoretically compelling

Motivation

- ① gravity at long distances
- ② galaxy rotation curves → "dark matter" [plot]
- ③ acceleration of universe → "dark energy" (p < 0) [plot]

② or: modify gravity?

(Leverrier... ) 1846: Uranus → Neptune  
mercury → "Vulcan" false dete until 1915

② Problem: difficult to modify gravity at long distances while keeping nucleus of GR

- compatible w/ special relativity
- ~~positive~~ no disastrous instability
- experiment
- Newtonian limit (equiv principle)
- Post-Newtonian tests

no detail here

already rules out most

① First attempt at modification:  
Branes - Dicks  
GR + scalar field

$$L_{\text{scalar}} = \frac{1}{2} \partial^\mu \phi \partial_\mu \phi \quad L_{\text{matt}} (g_{\mu\nu} \rightarrow A^2(\phi) g_{\mu\nu})$$

$$\ln A = \frac{\alpha_0}{\sqrt{8\pi G}} \left( \frac{\phi - \phi_0}{\sqrt{8\pi G}} + \frac{1}{2} \beta_0 \frac{(\phi - \phi_0)^2}{8\pi G} + \dots \right)$$

Ordinary scalar couples to matter in a particular way  
 looks not very well motivated — and it isn't from modern perspective  
 (Historically, motivated tests of GR (equivalence principle, etc.)

[Plot] Cassini: measured ~~the~~ Poppler shift of radio waves between Cassini satellite and earth passing near sun

$$\alpha_0 \approx 10^{-3}$$

~~Plot~~  $\Rightarrow$  very weak coupling to matter

$\sim$  "bending of light by sun"

~~MOND?~~  
 ④ Modern attempts (long distance mod)

Inspired by superconductivity

	<u>supercond</u>	<u>gravity</u>
--	------------------	----------------

long range force

E & M

gravity

symmetry

~~gauge invariance~~  
~~phase~~  
 gauge invariance

coordinate invariance  
 local Lorentz invariance

~~break~~ break symmetry  $\Rightarrow$  modification of long range forces

Also gravity + extra modes, but now motivates many ~~length~~ effects

- preferred frames ...
- new long-range forces, e.g. [plot] spin dependent  $\frac{1}{r^2}$  force

⑤ above driven ~~to~~ by theory:

~~to~~ How can we modify gravity  
Do not solve problems at long distance.

ask: how would we like to modify gravity?

⑥ ~~MOND~~ Dark matter ~~or~~ mod grav?  
MOND?  
Totally phenomenological, motivated by galaxy rot curve

Newton:  $r > R_{gal} \Rightarrow \frac{1}{2} m v^2 \sim \frac{1}{2} \frac{G M m}{r} \sim \frac{1}{2} \frac{G M m}{r^2} r^2$

~~$\frac{1}{2} m v^2 \sim \frac{1}{2} \frac{G M m}{r}$~~   
 ~~$v \sim \frac{1}{r}$~~   
 ~~$v \sim \frac{1}{r^2}$~~



~~MOND~~:

$a = \frac{v^2}{r} \approx \frac{F_{grav}}{m} \sim \frac{1}{r^2}$

$\Rightarrow v \sim r^{-1/2}$

MOND:  $F_{grav} \sim \frac{1}{r}$  when  $a_N < a_0 = \text{new const}$

Problem: not a theory! (How to test in lab?)

~~Bechenstein~~  
Evidence for DM from lensing of galaxies ~~at Bechenstein~~  
Bechenstein: "AQUAL" theory has many adjustable params ~~at Bechenstein~~ ...

Also: other evidence for DM

- lensing of galaxies ← especially hard for MOND
  - structure formation
- MOND: not a theory. (hard to test in lab)  
Bechenstein: keeps trying to make relativistic theory of MOND, but ~~very~~ requires many arbitrary params.

② CC - problem

Very fundamental qualitative problem

$$V \mapsto V + \text{const}$$

relativistic. what could it be?

Einstein:  $T_{\mu\nu} \mapsto T_{\mu\nu} + \text{const} \cdot g_{\mu\nu}$

GR

$$\rho = -p$$

QM: ~~Eg = ...~~

$$E_{\text{vac}} = \sum_{\text{modes}} \frac{1}{2} \hbar \omega = \infty ?$$

Good news: understand how it can be finite: SUSY! (cancellation between bosons & fermions)

Bad news: SUSY broken at energy scales  $\gtrsim 100 \text{ GeV}$   ~~$\sim 10^{16} \text{ GeV}$~~   ~~$\sim 10^{19} \text{ GeV}$~~   ~~$\sim 10^{28} \text{ GeV}$~~  (t=c=1)  ~~$\sim 10^8 \times p_{\text{nuclear}}$~~   $\sim 10^8 \text{ GeV} \approx \text{mpc}^2$

num cancellation  $\Rightarrow V_{\text{eff}} \gtrsim (10^{11} \text{ eV})^4 (10^2 \text{ GeV})^4 \approx 10^8 P_{\text{Nuclear}}$

~~What would be eff~~  
 $\Rightarrow$  spacetime  $\Rightarrow$  unresolvable expansion at rate

$H_{\text{eff}}^2 \sim G_N V_0 \sim H_0^2$

$H_0 \sim 10^{-18} \text{ s}^{-1} \Rightarrow H_{\text{eff}}^{-1} \sim \text{cm} \sim 10^{-8} \text{ s}$   
size of horizon       $\sim$  Hubble time

End of lecture  $\Rightarrow$  big trouble!

$\frac{H_0}{H_{\text{eff}}} \sim \frac{H_{\text{obs}}}{H_0} \sim \frac{10^{-18}}{10^{-42}} \sim 10^{24}$

$\frac{H_{\text{obs}}}{H_{\text{eff}}} \sim 10^{28} \Rightarrow \frac{V_{\text{obs}}}{V_{\text{th}}} \sim 10^{56}$

⑤ Problem: modify gravity so that vacuum energy does not gravitate

$V_{\text{vac}} \sim \sum_{\text{modes}} \frac{1}{2} \hbar \omega \sim \int \frac{d^3k}{(2\pi)^3} \frac{1}{2} \hbar \omega \sim \int \frac{d^3k}{(2\pi)^3} \frac{1}{2} \hbar c k \sim \Lambda^4$   
vacuum as source of gravity      form factor

$$\Lambda^4 \approx V_{\text{obs}} \quad V_{\text{obs}} \sim G_N H_{\text{obs}}$$

$$\rightarrow \Lambda \approx \left( \frac{H_{\text{obs}}^2}{G_N} \right)^{1/4} \sim 10^{-2} \text{ eV}$$

Expect modification of Newton force at distance

$$r \sim \frac{1}{\Lambda} \sim 10^2 \text{ eV} \sim 10^{-3} \text{ cm}$$

[Note  $\Lambda \downarrow \Rightarrow r \uparrow \Rightarrow$  no wiggle room!]

Expect that gravity becomes weaker at a micron....

Note: no model (grow hard to modify) but ~~idea~~ idea is sufficiently intriguing to keep in mind (and Muehler is working on an "existence proof...")

⑦ Large extra dim

Motivated by particle physics

$$M_W \sim 100 \text{ GeV}$$

$$M_P \sim \frac{1}{\sqrt{G_N}} \sim 10^{19} \text{ GeV}$$

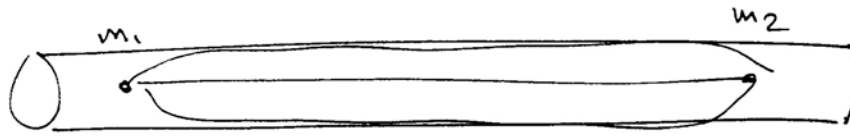
Why different?

Usual framework:  $M_P$  represents scale of new physics (quantum gravity, strings...)

ADD: 100 GeV is most fundamental scale  
largest scale

Then: how to ~~explain~~ explain weakness of gravity?

$$r \gg R : d=3$$



$$F_{\text{grav}} \sim \frac{1}{M_*^2} \frac{m_1 m_2}{r^2}$$

$$G_N \sim \frac{1}{M_*^2}$$

Match at  $r \sim R$ :  $D=4+n$

$$\frac{1}{M_*^{2+n}} \frac{1}{R^{2+n}} \sim \frac{1}{M_*^2 R^2}$$

$$M_*^2 \sim M_*^{2+n} R^n$$

~~$M_* \sim 100 \text{ GeV}$~~   $M_* \sim 1000 \text{ GeV}$   
 ~~$R \sim 10^{13} \text{ cm}$~~   $R \sim 10^8 \text{ cm}$

$n=1$  :  $R \sim 10^{13} \text{ cm} \sim \frac{1}{10} \text{ AU}$

$n=2$  :  $R \sim \text{mm}$  ~~test this~~

$n=3$  :  $R \sim 10^{-7} \text{ cm} \sim 10 \text{ \AA}$

⋮

gravity gets stronger at mm.  
 specific model  $\Rightarrow$  can really constrain it.

[plot]