

## 21 Stat Mech of Ideal Gas

Density of states as function of E and of  $|k|$ ;  $\tilde{g}(k)dk \sim L^d k^{d-1} dk$ ;  $g(E)dE = \tilde{g}(k(E)) (dk/dE) dE$

$E \propto k^2$  for particles (with mass),  $E \propto k$  for photons, phonons (no rest mass)

$\lambda_{th}$   $Z_1 = V/\lambda_{th}^3$   $Z_N = Z_1^N/N!$  Then find F, U, S = (U-F)/T, C

## 22 Chemical potential

Definition, meaning; for ideal gas  $\mu = k_B T \ln(n \lambda_{th}^3)$

Gibbs distribution  $P_i = Z^{-1} \exp[\beta(\mu N_i - E_i)]$

Ensembles: microcanonical, canonical, grand canonical

$\mu$  and chemical reactions;  $\mu(p)$  and reference  $\mu$  and  $p$ ; equilibrium constant K

## 23 (NOT 23.7) Photons

Stefan-Boltzmann law, spectral energy density, power received by earth from sun, radiation pressure,

$g(\omega)$  for photons, black-body distribution, Wien's law

Einstein A & B coefficients, NOT cosmic background radiation

## 24 (NOT 24.3) Phonons

Einstein model, assumptions, results, C

Debye model (interacting particles), assumptions, results, C

NOT phonon dispersion

## 26 (NOT 26.2, pp. 291-3) Real gases: van der Waals gas: eqn of state, partition function

Coexistence and metastable states, Gibbs construction, NOT Dieterici eqn.

Law of corresponding states, basics of virial expansion

## 28 Phase transitions (NOT 28.5, 28.6)

Latent heat, Clausius-Clapeyron

Chemical potential as function of T or p NOT Gibbs phase rule, colligative properties

First-order vs. continuous phase transitions; how to tell

## 29 Fermi-Dirac and Bose-Einstein distribution functions and partition functions

$g(E)$  for massive particles in various dimensions

N & U for bosons in terms of  $\text{Li}_n(z)$ ; fugacity z

Ground state (T=0) of Fermi gas

Sommerfeld expansion and its uses for  $kT$  "small"

$$\int_0^\infty \phi(E) f_{FD}(E) dE = \int_0^{E_F} \phi(E) dE + \frac{\pi^2}{6} (k_B T)^2 \left[ \phi'(E_F) - \phi(E_F) \frac{g'(E_F)}{g(E_F)} \right]$$

Bose gas and Bose-Einstein condensation

General: Know low-T behavior of heat capacity C for all cases

*Some important topics from previous tests, for review*

Various views of pressure

Maxwell-Boltzmann distribution

Mean free path and collisions

Laws 0, 1, 2, 3 of thermodynamics

Adiabatic, isothermal, isobaric, and isochoric processes; Carnot cycle

Equipartition, for quadratic and non-quadratic modes