

An object falling in air satisfies the ordinary differential equation gotten from N2:

$$m \frac{dv}{dt} = -mg - bv$$

The equation has three dimensioned parameters ( $m$ ,  $g$ , and  $b$ ) and one dimensioned variable ( $v$ ).

- (a) Use the fixed dimensioned parameters in this equation to create “natural” scales of mass, length, and time,  $M_0$ ,  $L_0$ , and  $T_0$ .
- (b) Using these scales, create a natural scale for the velocity,  $V_0$ .
- (c) Define a dimensionless velocity  $V$  by the equation  $V=v/V_0$ .
- (d) Rewrite the original equation for  $v$  as an equation for  $V$ . This equation should contain no parameters that have any dimensions (or perhaps only combinations of parameters that have no dimensions).