

Initial value constraint:

Maxwell's: $\partial_\mu F^{\mu\nu} = 4\pi j^\nu \rightarrow \partial_\nu \partial_\mu F^{\mu\nu} \equiv 0$

so $\partial_0 (\partial_\mu F^{\mu 0}) = 0 \rightarrow \partial_\mu F^{\mu 0}$ only has 1st derivatives on t
can only have 2nd derivatives on t

In GR: $G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2}R g_{\mu\nu}$, $\nabla^\mu G_{\mu\nu} \equiv 0$ (contracted Bianchi identity)

in a coord $(x^0, x^i) \mid \frac{\partial}{\partial x^0}$ is time like, $\partial^0 G_{0\nu}$ must contain no 3rd time derivatives
(to be able to cancel)

so $G_{0\nu}$ contains no 2nd time derivatives.

$\Rightarrow \boxed{G_{0\nu} = 8\pi G T_{0\nu}}$ contains no 2nd time derivatives $\Rightarrow$ 4 initial value constraints eqns.