

So: $\nabla_a \nabla_b \xi_c = -\nabla_b \nabla_c \xi_a - \nabla_c \nabla_a \xi_b$

$$= -\nabla_b \nabla_c \xi_a + \nabla_c \nabla_b \xi_a = -R_{bca}{}^d \xi_d$$

→ $\boxed{\nabla_a \nabla_b \xi_c = -R_{bca}{}^d \xi_d}$, 2nd derivatives of ξ_μ are defined by

$$\xi_\mu|_p \text{ and } \nabla \xi|_p, \text{ for a particular } p.$$

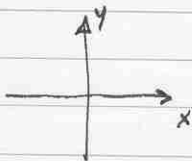
• So can only choose freely $\boxed{\xi_a}$ and $\boxed{\nabla_a \xi_b}$ at a given point. ~~✗~~

then ξ_a is determined everywhere else. → there's almost no solns.

How much freedom? $4 + 6 = 10$ (locally)

But if try to ~~insert~~ integrate for a general spacetime, likely will find no soln.

ex:



$$\partial_i \xi_j + \partial_j \xi_i = 0$$

$$\partial_x \xi_x = 0 \longrightarrow \xi_x = f(y) = \overset{\text{rotation}}{-cy} + \overset{\text{translations}}{d}$$

$$\partial_y \xi_y = 0 \longrightarrow \xi_y = g(x) = \overset{\text{translations}}{cx} + \overset{\text{rotation}}{e}$$

$$\partial_x \xi_y + \partial_y \xi_x = 0 \longrightarrow \frac{dg}{dx} = -\frac{df}{dy} = c$$