

d) Suppose  $A = e^B$  and  $\tilde{B} = -B$ .

$$\text{Then } \tilde{A} = \left( \sum \frac{B^n}{n!} \right) = \sum \frac{\tilde{B}^n}{n!} = e^{\tilde{B}}.$$

$$\text{But } \tilde{B} = -B \Rightarrow e^{\tilde{B}} = e^{-B} = A^{-1}.$$

$$\therefore \boxed{\tilde{A} = A^{-1}}$$

e) Suppose  $A = e^{iB}$ , and  $B^\dagger = B$ .

$$\text{Then } A^\dagger = \left( \sum \frac{(iB)^n}{n!} \right)^\dagger = \sum \frac{\{(iB)^\dagger\}^n}{n!}$$

$$= e^{(iB)^\dagger} = e^{-iB^\dagger}. \quad \text{But } B^\dagger = B \Rightarrow$$

$$e^{-iB^\dagger} = e^{-iB} = A^{-1}.$$

$$\therefore \boxed{A^\dagger = A^{-1}}$$