

Suppose we set our clocks so that the mass reaches the water at $t=0$. Then $t_0=0$, and we have

$$z(t) = A [1 - \cos(\omega t)].$$

What is A ? There are two ways to find out:

a) We have

$$\ddot{z} = \omega^2 A \cos(\omega t)$$

and we will have $\ddot{z} = 0$ when $\omega t = \pi/2$,
and then

$$z = A [1 - \cos(\pi/2)] = A.$$

We know that this is also the equilibrium height because then $F = 0 \Rightarrow \ddot{z} = 0$.

Thus, $A = 22.75$ meters.

b) Alternatively, we have

$$\ddot{z} = \omega^2 A \cos(\omega t) \quad \text{and} \quad z|_{t=0} = 0.$$

Thus $\ddot{z}|_{t=0} = \omega^2 A = \text{acceleration when}$