

Dragt 42 cont. Now square both sides to get

3/8

$$(Mga - ka^2)^2 \cos^2 \theta_0 = (ka\lambda_0)^2 \cos^2 (\pi/4 - \theta_0/2) = (ka\lambda_0)^2 [1 + \cos(\pi/2 - \theta_0)]/2$$

or,  $(Mga - ka^2)^2 (1 - \sin^2 \theta_0) = (ka\lambda_0)^2 (1 + \sin \theta_0)/2 \Rightarrow$

$$2(Mga - ka^2)^2 (1 - \sin \theta_0) = (ka\lambda_0)^2 \Rightarrow$$

$$\sin \theta_0 = 1 - \frac{(ka\lambda_0)^2}{2(Mga - ka^2)^2}$$

b) Suppose  $\theta_0 = 0$ . Then  $2(Mga - ka^2)^2 = (ka\lambda_0)^2$  or

$Mga - ka^2 = \pm (ka\lambda_0)/\sqrt{2}$ . But, from the earlier relation

$$Mga \cos \theta_0 - ka \cos(\pi/4 - \theta_0/2) [2a \sin(\pi/4 - \theta_0/2) - \lambda_0] = 0$$
 we get for

$$Mga - ka \cos(\pi/4) [2a \sin(\pi/4) - \lambda_0] = 0 \quad \text{or}$$

$$Mga - ka \frac{1}{\sqrt{2}} \left( \frac{2a}{\sqrt{2}} - \lambda_0 \right) = 0 \quad \text{or} \quad Mga - ka^2 + \frac{ka\lambda_0}{\sqrt{2}} = 0$$