

$$\frac{\partial L}{\partial \theta} = -Mg a \cos \theta - k [2a \sin(\pi/4 - \frac{\theta}{2}) - l_0] 2a \cos(\pi/4 - \frac{\theta}{2}) (-\frac{1}{2}).$$

So the equation of motion becomes

$$Ma^2 \ddot{\theta} + Mg a \cos \theta - k a \cos(\pi/4 - \frac{\theta}{2}) [2a \sin(\pi/4 - \frac{\theta}{2}) - l_0] = 0$$

Assume $\theta = \theta_0$ is an equilibrium solution. Then one must have

$$Mg a \cos \theta_0 - k a \cos(\pi/4 - \theta_0/2) [2a \sin(\pi/4 - \theta_0/2) - l_0] = 0$$

Work on this eqn to solve for θ_0 . One finds

$$Mg a \cos \theta_0 = 2ka^2 \sin(\pi/4 - \theta_0/2) \cos(\pi/4 - \theta_0/2) - k a l_0 \cos(\pi/4 - \theta_0/2)$$

$$= ka^2 \sin(\pi/2 - \theta_0) - k a l_0 \cos(\pi/4 - \theta_0/2) \Rightarrow$$

$$(Mg a - ka^2) \cos \theta_0 = -k a l_0 \cos(\pi/4 - \theta_0/2).$$