

$$\mathcal{L} = \frac{1}{2} m \vec{v} \cdot \vec{v} + q \vec{v} \cdot \vec{A}$$

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$$= \frac{1}{2} m [\dot{\rho}^2 + \rho^2 \dot{\phi}^2 + \dot{z}^2] + q \frac{\rho \dot{\phi} \mu \rho}{[\rho^2 + z^2]^{3/2}} \Rightarrow$$

$$\mathcal{L} = \frac{1}{2} m [\dot{\rho}^2 + \rho^2 \dot{\phi}^2 + \dot{z}^2] + \frac{q \mu \rho^2 \dot{\phi}}{[\rho^2 + z^2]^{3/2}}$$

$$b) p_{\rho} = \frac{\partial \mathcal{L}}{\partial \dot{\rho}} = m \dot{\rho} \Rightarrow m \ddot{\rho} = \frac{\partial \mathcal{L}}{\partial \rho} \Rightarrow$$

$$m \ddot{\rho} = m \rho \dot{\phi}^2 + q \mu \dot{\phi} \frac{\partial}{\partial \rho} \frac{\rho^2}{[\rho^2 + z^2]^{3/2}}$$

$$p_{\phi} = \frac{\partial \mathcal{L}}{\partial \dot{\phi}} = m \rho^2 \dot{\phi} + \frac{q \mu \rho^2}{[\rho^2 + z^2]^{3/2}} \Rightarrow$$

$$\dot{p}_{\phi} = \frac{\partial \mathcal{L}}{\partial \phi} = 0 \Rightarrow m \rho^2 \dot{\phi} + \frac{q \mu \rho^2}{[\rho^2 + z^2]^{3/2}} = \text{const}$$

$$p_z = \frac{\partial \mathcal{L}}{\partial \dot{z}} = m \dot{z} \Rightarrow m \ddot{z} = \frac{\partial \mathcal{L}}{\partial z} \Rightarrow$$

$$m \ddot{z} = q \mu \rho^2 \dot{\phi} \frac{\partial}{\partial z} \frac{1}{[\rho^2 + z^2]^{3/2}}$$