

$$\vec{L}_{cm}^2 \log \left[ \frac{1}{S(t_2)} \right] \leq -\vec{L}_{cm}^2 \log S(t_1) + 4W \int_{t_1}^{t_2} \dot{S} dt' - 4 \int_{t_1}^{t_2} \dot{S} \ddot{S} dt'$$

But  $-4 \int_{t_1}^{t_2} \dot{S} \ddot{S} dt' = -2 \dot{S}^2 \Big|_{t_1}^{t_2} = 2\dot{S}^2(t_1) - 2\dot{S}^2(t_2) \leq 2\dot{S}^2(t_1)$

$$4W \int_{t_1}^{t_2} \dot{S} dt' = 4W [S(t_2) - S(t_1)]$$

$$\therefore \vec{L}_{cm}^2 \log \left[ \frac{1}{S(t_2)} \right] \leq -\vec{L}_{cm}^2 \log S(t_1) + 4W [S(t_2) - S(t_1)] + 2\dot{S}^2(t_1)$$

Let  $C \equiv -\vec{L}_{cm}^2 \log S(t_1) - 4WS(t_1) + 2\dot{S}^2(t_1)$

Then we get

$$(F) \quad \vec{L}_{cm}^2 \leq \frac{4WS(t_2) + C}{\log \left( \frac{1}{S(t_2)} \right)}$$

Also, we know  $\vec{L}_{cm}^2 \geq 0$ .

Letting

$t_2 \rightarrow t_c$  gives  $\vec{L}_{cm} = 0$ , which

means that only under this exceptional condition may all the bodies collide.