

DCM 1.18 continued

2/2

c) Divide the result of part b by m_{sun} to get

$$\frac{M}{m_{\text{sun}}} = \frac{r^* v^{*2}}{G m_{\text{sun}}}. \quad \text{For the earth sun system}$$

$$m_{\text{earth}} \omega^2 R = \frac{G m_{\text{earth}} m_{\text{sun}}}{R^2} \quad \text{where } R = \text{distance from sun to earth}$$

$$\Rightarrow \boxed{\frac{M}{m_{\text{sun}}} = \frac{r^* v^{*2}}{\omega^2 R^3}}$$

$$r^* = 32.6 \text{ light years}$$

$$v^* = 7.65 \text{ km/sec}$$

$$R = 500 \text{ light sec}, \quad \omega = \frac{2\pi}{1 \text{ yr}} = \frac{2\pi}{60 \cdot 60 \cdot 24 \cdot 365} = 1.992 \times 10^{-7} \text{ sec}^{-1}$$

$$r^* = 32.6 \text{ light yrs} = 32.6 \times 60 \cdot 60 \cdot 24 \cdot 365 = 1.028 \times 10^9 \text{ light sec}$$

$$v^* = 7.65 \text{ km/sec} = \frac{7.65}{3 \times 10^5} = 2.55 \times 10^{-5} \text{ light sec/sec}$$

$$\frac{M}{m_{\text{sun}}} = \frac{1.028 \times 10^9 \cdot (2.55 \times 10^{-5})^2}{(1.992 \times 10^{-7})^2 (500)^3} = \frac{6.685 \times 10^{-1}}{4.96 \times 10^{-6}}$$

$$= 1.35 \times 10^5$$