

Then we get

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$$\mu = -(1/4)(e^{2\phi} - 1)^2 = \frac{1}{4} e^{2\phi} [2 - 2\cos\theta]$$

$$= (1/4) \cos\phi [2 - 2\cos\theta] + \frac{1}{4} \times \sin\theta [2 - 2\cos\theta]$$

$$= x + iy$$

with $x = \frac{1}{4} \cos\phi [2 - 2\cos\theta], y = \frac{1}{4} \sin\theta [2 - 2\cos\theta].$

Normally in polar coordinates we have

$$x = \rho \cos\phi, y = \rho \sin\phi \Rightarrow y/x = \tan\phi. \text{ Here we}$$

$$\text{have } y/x = \frac{\frac{1}{4} \sin\theta [2 - 2\cos\theta]}{\frac{1}{4} \cos\phi [2 - 2\cos\theta]} = \tan\phi! \text{ So, } \phi$$

is a polar angle. Evidently we have

$$\rho = |\mu| = \frac{1}{4} |2 - 2\cos\theta| = \frac{1}{2} (1 - \cos\theta)$$

The equation of a cardioid is

$$x^2 + y^2 + \frac{1}{2}x = \frac{1}{2} \sqrt{x^2 + y^2}$$

See the attached page.