

$$\text{In[37]:= } \left( \chi = \left\{ \left( \text{Cos}[\lambda t / 2] + \text{I} \frac{(\omega + \omega 1 \text{Cos}[\alpha])}{\lambda} \text{Sin}[\lambda t / 2] \right) \text{E}^{-\text{I} \omega t / 2}, \right. \right. \\ \left. \left. \left( \text{I} \omega 1 \frac{\text{Sin}[\alpha]}{\lambda} \text{Sin}[\lambda t / 2] \right) \text{E}^{\text{I} \omega t / 2} \right\} \right) // \text{MatrixForm}$$

Out[37]//MatrixForm=

$$\left( \begin{array}{c} e^{-\frac{1}{2} i t \omega} \left( \text{Cos} \left[ \frac{t \lambda}{2} \right] + \frac{i (\omega + \omega 1 \text{Cos}[\alpha]) \text{Sin} \left[ \frac{t \lambda}{2} \right]}{\lambda} \right) \\ \frac{i e^{\frac{i t \omega}{2}} \omega 1 \text{Sin}[\alpha] \text{Sin} \left[ \frac{t \lambda}{2} \right]}{\lambda} \end{array} \right)$$

$$\text{In[51]:= } \left( \mathbf{H} = \mathbf{e} \mathbf{h} \frac{\mathbf{B}}{2 m} \left\{ \left\{ \text{Cos}[\alpha], \text{Sin}[\alpha] \text{E}^{-\text{I} \omega t} \right\}, \left\{ \text{Sin}[\alpha] \text{E}^{\text{I} \omega t}, -\text{Cos}[\alpha] \right\} \right\} \right) // \text{MatrixForm}$$

Out[51]//MatrixForm=

$$\left( \begin{array}{cc} \frac{\text{B e h Cos}[\alpha]}{2 m} & \frac{\text{B e e}^{-i t \omega} \text{h Sin}[\alpha]}{2 m} \\ \frac{\text{B e e}^{i t \omega} \text{h Sin}[\alpha]}{2 m} & -\frac{\text{B e h Cos}[\alpha]}{2 m} \end{array} \right)$$

$$\text{In[52]:= } \text{Simplify} \left[ \left( \mathbf{I} \mathbf{h} \mathbf{D}[\chi, t] \right) // . \left\{ \lambda \rightarrow \text{Sqrt}[\omega^2 + \omega 1^2 + 2 \omega \omega 1 \text{Cos}[\alpha]], \omega 1 \rightarrow -e \frac{\mathbf{B}}{m} \right\} \right] // \text{MatrixForm}$$

$$\text{Simplify} \left[ \left( \mathbf{H} \cdot \chi \right) // . \left\{ \lambda \rightarrow \text{Sqrt}[\omega^2 + \omega 1^2 + 2 \omega \omega 1 \text{Cos}[\alpha]], \omega 1 \rightarrow e \frac{\mathbf{B}}{m} \right\} \right] // \text{MatrixForm}$$

$$\text{Simplify} \left[ \left( \mathbf{I} \mathbf{h} \mathbf{D}[\chi, t] - \mathbf{H} \cdot \chi \right) // . \left\{ \lambda \rightarrow \text{Sqrt}[\omega^2 + \omega 1^2 + 2 \omega \omega 1 \text{Cos}[\alpha]], \omega 1 \rightarrow -e \frac{\mathbf{B}}{m} \right\} \right] //$$

**MatrixForm**

Out[52]//MatrixForm=

$$\left( \frac{\text{B e e}^{-\frac{1}{2} i t \omega} \text{h} \left( -i \text{B e Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + \text{Cos}[\alpha] \left( m \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \text{Cos} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + i m \omega \text{Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] \right)}{2 m^2 \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}}} \right. \\ \left. \frac{\text{B e e}^{\frac{i t \omega}{2}} \text{h Sin}[\alpha] \left( \text{Cos} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + \frac{i \omega \text{Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right]}{\sqrt{\frac{\text{B}^2 e^2 + \omega^2 - 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}}} \right)}{2 m} \right)$$

Out[53]//MatrixForm=

$$\left( \frac{\text{B e e}^{-\frac{1}{2} i t \omega} \text{h} \left( i \text{B e Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + \text{Cos}[\alpha] \left( m \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \text{Cos} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + i m \omega \text{Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] \right)}{2 m^2 \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}}} \right. \\ \left. \frac{\text{B e e}^{\frac{i t \omega}{2}} \text{h Sin}[\alpha] \left( \text{Cos} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right] + \frac{i \omega \text{Sin} \left[ \frac{1}{2} t \sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}} \right]}{\sqrt{\frac{\text{B}^2 e^2 + \omega^2 + 2 \text{B e} \omega \text{Cos}[\alpha]}{m^2}}} \right)}{2 m} \right)$$

Out[54]//MatrixForm=

$$\left( \begin{array}{c} 0 \\ 0 \end{array} \right)$$

$$\begin{aligned}
\text{In[55]:= } & \text{Series}\left[\chi /. \left\{ \text{Cos}[\alpha] \rightarrow \text{Sqrt}[1 - \text{sin}\alpha^2], \text{Sin}[\alpha] \rightarrow \text{sin}\alpha, \right. \right. \\
& \left. \left. \omega 1 \rightarrow -e \frac{\mathbf{B}}{\mathbf{m}}, \lambda \rightarrow \text{Sqrt}[\omega^2 + \omega 1^2 + 2 \omega \omega 1 \text{Sqrt}[1 - \text{sin}\alpha^2]] \right\}, \{\text{sin}\alpha, 0, 2\} \right] \\
\text{Out[55]= } & \left\{ e^{-\frac{1}{2} i t \omega} \left( \text{Cos}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right] + \frac{i (-\mathbf{B} e + \mathbf{m} \omega) \text{Sin}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right]}{\mathbf{m} \sqrt{(\omega + \omega 1)^2}} \right) + \right. \\
& e^{-\frac{1}{2} i t \omega} \left( \frac{t \omega \omega 1 \text{Sin}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right]}{4 \sqrt{(\omega + \omega 1)^2}} + i \left( -\frac{t \omega \left(-\frac{\mathbf{B} e}{\mathbf{m}} + \omega\right) \omega 1 \text{Cos}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right]}{4 \sqrt{(\omega + \omega 1)^2} \sqrt{\omega^2 + 2 \omega \omega 1 + \omega 1^2}} + \right. \right. \\
& \left. \left. \left( \frac{\omega \left(-\frac{\mathbf{B} e}{\mathbf{m}} + \omega\right) \omega 1}{2 \left((\omega + \omega 1)^2\right)^{3/2}} + \frac{\mathbf{B} e}{2 \mathbf{m} \sqrt{\omega^2 + 2 \omega \omega 1 + \omega 1^2}} \right) \text{Sin}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right] \right) \right) \text{sin}\alpha^2 + \\
& \left. \mathcal{O}[\text{sin}\alpha]^3, -\frac{i \mathbf{B} e e^{\frac{i t \omega}{2}} \text{Sin}\left[\frac{1}{2} t \sqrt{(\omega + \omega 1)^2}\right] \text{sin}\alpha}{\mathbf{m} \sqrt{(\omega + \omega 1)^2}} + \mathcal{O}[\text{sin}\alpha]^3 \right\}
\end{aligned}$$