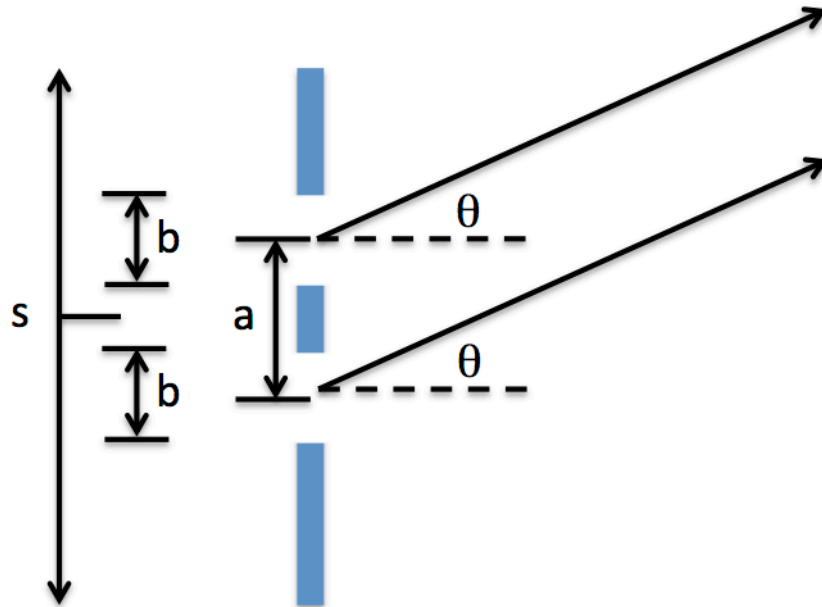


## Homework #12 - Phys 273

1) Consider a two-slit diffraction experiment with the following geometry:



The electric field amplitude on a distant screen ( $E_p$ ) at angle ( $\theta$ ) is determined by integrating over the slits:

$$E_p = \frac{E_L}{r_0} e^{i(kr_0 - \omega t)} \left[ \int_{-(a+b)/2}^{-(a-b)/2} e^{iks \sin \theta} ds + \int_{(a-b)/2}^{(a+b)/2} e^{iks \sin \theta} ds \right]$$

where ( $a$ ) is the distance between the slits and ( $b$ ) is the slit width. Evaluate the integrals and show that

$$E_p = \frac{2E_L b}{r_0} e^{i(kr_0 - \omega t)} \frac{\sin \beta}{\beta} \cos \alpha$$

where  $\alpha = \frac{1}{2} ka \sin \theta$ ,  $\beta = \frac{1}{2} kb \sin \theta$ .

2) Sketch the diffraction patterns that you would observe on a screen 1 m from an aperture illuminated by a He-Ne laser (wavelength = 633 nm), for the following cases:

- a) a single slit, with slit width = 20 microns.
- b) two slits, slit width = 20 microns, slit spacing = 80 microns.

Draw these diffraction patterns as a function of position on the screen, with the x-axis in units of meters, and label the position of the first zero due to the "slit width" term.

*(more problems on the next page)*

3) **Michelson-Morley experiment.** Imagine that a Michelson interferometer is oriented so that one arm points in the direction of earth's motion around the sun, and that the other arm is transverse to the earth's motion. The interferometer is illuminated with a He-Ne laser, with wavelength 633 nm, and the length of each arm is ten meters. Six hours later, both arms are perpendicular to the earth's motion, because the earth has rotated.

If we were to assume, incorrectly, that the speed of light for motion parallel to the earth's velocity is  $(c + v_e)$ , and the speed of light perpendicular to the earth's motion is simply  $(c)$ , how many fringes would we expect to observe pass by on the screen during the six hours that it takes the earth to rotate from the first configuration to the second?  $(c)$  is the speed of light in vacuum ( $3.0 \times 10^8$  m/s), and  $(v_e)$  is the Earth's orbital velocity around the sun, which is  $3.0 \times 10^4$  m/s.

*Remark: As you may know, when this experiment is actually performed, no fringe shift is observed because the velocity of light is independent of the frame of reference. This is a basic feature of the theory of special relativity.*