

$$E_0 = E_c$$

$$Mg \frac{r}{2} (1 - \cos \theta_f) + mg r (1 - \cos \theta_f) = \frac{1}{2} (I + m r^2) \omega_c^2$$

$$(\frac{1}{2} M + m) g r (1 - \cos \theta_f) = \frac{1}{2} (\frac{3}{2} M + m) r^2 \omega_c^2$$

$$1 - \cos \theta_f = \frac{1}{2} \frac{\frac{3}{2} M + m}{\frac{1}{2} M + m} \frac{r}{g} \omega_c^2$$

$$\cos \theta_f = 1 - \frac{1}{2} \frac{\frac{3}{2} M + m}{\frac{1}{2} M + m} \frac{r}{g} \omega_c^2 = 0.9957$$

$$\Rightarrow \theta_f = 5.3^\circ$$

Problem 2

$$(a) F = \text{const} \Rightarrow W = F \cdot d$$

$$W = \Delta K$$

$$F \cdot d = \frac{1}{2} M v^2 + \frac{1}{2} I \omega^2$$

$$= \frac{1}{2} M v^2 + \frac{1}{2} (M R^2) \left(\frac{v}{R} \right)^2$$

$$\omega = \frac{v}{R} \quad \text{rolling w/o slipping}$$

$$\Rightarrow v^2 = \frac{F}{M} d = M v^2$$

(b) Const acceleration from rest

$$v^2 = 2ad \Rightarrow 2a = \frac{F}{M} \quad a = \frac{1}{2} \frac{F}{M}$$