

$T_1 = T_2$ if $m_{\text{scale}} = 0$ (massless string)

$$N2: a_1 = \frac{T_1 - m_1 g}{m_1} = \frac{T - m_1 g}{m_1}$$

$$a_2 = \frac{T_2 - m_2 g}{m_2} = \frac{T - m_2 g}{m_2}$$

Move together: $a_1 = -a_2$

Elim T: $T = m_1 a_1 + m_1 g = m_1 (a_1 + g)$

$$a_1 = -a_2 = -\frac{T - m_2 g}{m_2} = -\frac{m_1 (a_1 + g) - m_2 g}{m_2}$$

~~$$(m_2 - m_1) a_1 = (m_1 - m_2) g$$~~

~~$$a_1 =$$~~
$$(m_2 + m_1) a_1 = -m_1 g + m_2 g$$

$$a_1 = \frac{m_2 - m_1}{m_1 + m_2} g$$

Reality checks:

dimensions ☒

$$m_1 > m_2 \Rightarrow a_1 < 0 \quad \checkmark$$

$$m_1 = m_2 \Rightarrow a_1 = 0 \quad \checkmark$$

⋮

$$(b) T = m_1 (a_1 + g) = m_1 \left[\frac{m_2 - m_1}{m_1 + m_2} + 1 \right] g$$

$$= m_1 \frac{m_2 - \cancel{m_1} + (\cancel{m_1} + m_2)}{m_1 + m_2} g$$

$$T = \frac{2m_1 m_2}{m_1 + m_2} g = 1.04 \text{ N} = \text{scale reading}$$