

6. During a small period of time Δt , the mass of the cart changes
 $\Delta m = A \Delta t$, here $A = 1.2 \text{ kg/s}$.

The momentum before Δt and after Δt is P_0 . P_0 is constant due to momentum conservation.

Then $P_0 = mv \Rightarrow v = \frac{P_0}{m}$

$$a = \frac{dv}{dt} = P_0 \frac{d\left(\frac{1}{m}\right)}{dt} = -\frac{P_0}{m^2} \frac{dm}{dt} = -\frac{P_0 A}{m^2} = -\frac{mvA}{m^2}$$

$$= -\frac{Av}{m}$$

So $a = -1.2 \times 0.54 / 21 = -0.03 \text{ m/s}^2$ at a certain instant.

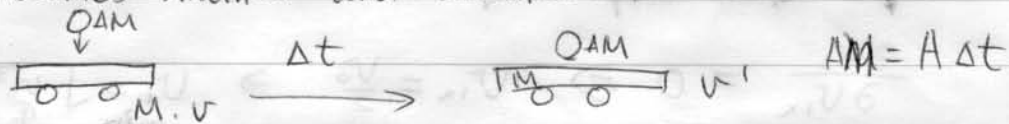
from $a = -\frac{P_0 A}{m^2}$ $m = m_0 + At$

$$a = -P_0 A (m_0 + At)^{-2}$$

$$= -13.608 (21 + 1.2t)^{-2}$$

So $|a|$ becomes smaller and smaller.

Another way,



$$F = \frac{\Delta p}{\Delta t} \quad \Delta p = mv' - mv = m(v' - v) \quad (m + \Delta m)v' = m \cancel{v}$$

$$F = \frac{m \left(\frac{m}{m + \Delta m} - 1 \right) v}{\Delta t} = -\frac{\Delta m v}{\Delta t} = -Av$$

$$= ma \Rightarrow a = \frac{F}{m} = -\frac{Av}{m} \text{ get the same result.}$$