

$$4. (a) \quad I = I_0 + MR^2 \\ = \frac{MR^2}{2} + M \cdot \left(\frac{R}{2}\right)^2 = \frac{3}{4}MR^2$$

(b)



Mg, gravity, give rise to nonzero torque.

(c) Newton's 2nd law

$$\begin{cases} Mg - T = Ma \\ Mg \times \frac{R}{2} = \frac{3}{4}MR^2\alpha \\ a = \frac{R}{2}\alpha \end{cases} \Rightarrow \begin{cases} Mg - T = Ma \\ 2g = 3R\alpha \Rightarrow a = \frac{g}{3} \\ R\alpha = 2a \end{cases}$$

(d) Energy conservation:

$$Mgh = \frac{1}{2}Mv^2 + \frac{1}{2} \left(\frac{v}{\frac{R}{2}}\right)^2 \cdot \frac{I_0}{2} \left(\frac{v}{\frac{R}{2}}\right)^2$$

$$Mgh = \frac{1}{2}Mv^2 + \frac{1}{2} \cdot \frac{MR^2}{2} \cdot \left(\frac{v}{\frac{R}{2}}\right)^2$$

$$v = \sqrt{\frac{2gh}{3}}$$

$$\begin{aligned} (e) \quad a &= \frac{dv}{dt} = \sqrt{\frac{2g}{3}} \frac{dh^{1/2}}{dt} = \sqrt{\frac{2g}{3}} \cdot \frac{1}{2} h^{-1/2} v \\ &= \sqrt{\frac{2g}{3}} \cdot \frac{1}{2} h^{-1/2} \cdot \sqrt{\frac{2gh}{3}} \\ &= \frac{1}{2} \cdot \frac{2g}{3} = \frac{g}{3} \end{aligned}$$

It agrees with the result from part (c).