

Useful Formulas - Exam II

Motion definitions

displacement:	$\Delta \mathbf{r} \equiv \mathbf{r}_f - \mathbf{r}_i$	
velocity:	average, $\bar{\mathbf{v}} \equiv \frac{\Delta \mathbf{r}}{\Delta t}$	instantaneous, $\mathbf{v} \equiv \frac{d\mathbf{r}}{dt}$
acceleration:	average, $\bar{\mathbf{a}} \equiv \frac{\Delta \mathbf{v}}{\Delta t}$	instantaneous, $\mathbf{a} \equiv \frac{d\mathbf{v}}{dt}$
radial acceleration:	$a_r = \frac{v^2}{r}$	
tangential acceleration:	$a_t = \frac{d \mathbf{v} }{dt}$	

Kinematic equations ($\mathbf{a}$ is constant)

$$\begin{aligned}\mathbf{v}_f &= \mathbf{v}_i + \mathbf{a} t & v_f^2 &= v_i^2 + 2 \mathbf{a} \cdot \mathbf{r} \\ \mathbf{r}_f &= \mathbf{r}_i + \mathbf{v}_0 t + \frac{1}{2} \mathbf{a} t^2 & \mathbf{r}_f &= \mathbf{r}_i + \frac{1}{2} (\mathbf{v}_i + \mathbf{v}_f) t\end{aligned}$$

Trigonometric formulas

$$\begin{aligned}\sin(\theta) &= \frac{\text{opp}}{\text{hyp}} & \text{Law of sines: } \frac{\sin(\alpha)}{a} &= \frac{\sin(\beta)}{b} = \frac{\sin(\gamma)}{c} \\ \cos(\theta) &= \frac{\text{adj}}{\text{hyp}} & \text{Law of cosines: } c^2 &= a^2 + b^2 - 2 a b \cos(\gamma) \\ \tan(\theta) &= \frac{\text{opp}}{\text{adj}}\end{aligned}$$

Identities

$$\begin{aligned}\sin^2(\theta) + \cos^2(\theta) &= 1 & \sin(A \pm B) &= \sin(A) \cos(B) \pm \cos(A) \sin(B) \\ \sin(2\theta) &= 2 \sin(\theta) \cos(\theta) & \cos(A \pm B) &= \cos(A) \cos(B) \mp \sin(A) \sin(B) \\ \cos(2\theta) &= \cos^2(\theta) - \sin^2(\theta)\end{aligned}$$