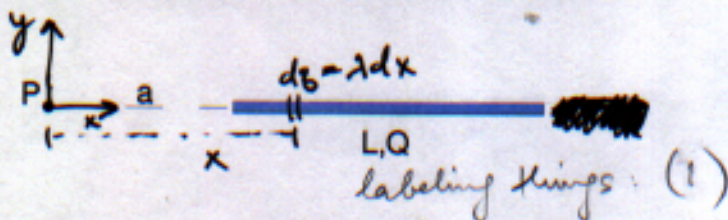


(10)

2. (a) Calculate the electric potential at point P (which is at the origin), due to the charged rod with length  $L$  and the total charge  $Q$ ; the rod is a distance  $a$  from the origin (see picture). (b) If I put a charge  $q$  at point P, what will be its electric potential energy (with respect to the rod)? (c) What is the direction of the electric field at point P, assuming that the charge  $Q$  is negative? (d) How would you set up the calculation of its magnitude? (you don't actually have to calculate it)



$$a) \quad (2) \quad V = k \int_0^Q \frac{dq}{x} \quad dq = \lambda dx$$

$$\text{add (1)} \quad V = k \int_a^{a+L} \frac{\lambda dx}{x}$$

$$V = k\lambda \ln(x) \Big|_a^{a+L}$$

$$V = k \frac{Q}{L} \ln\left(\frac{a+L}{a}\right)$$

$$\text{add (1)} \quad \boxed{V = k \frac{Q}{L} \ln\left(1 + \frac{L}{a}\right)}$$

$$b) \quad \boxed{U = qV} \quad (1) \quad \text{either } U = kq \frac{Q}{L} \ln\left(1 + \frac{L}{a}\right)$$

$$c) \quad \boxed{\vec{E} = E_x \hat{x}} \quad \text{-- in positive x-direction (toward the rod)} \quad (2)$$

$$d) \quad \text{either: } \boxed{\vec{E}_x = -\frac{dV}{dx}} \quad (2) \quad \leftarrow \text{either or}$$

$$\text{or: } \boxed{\vec{E} = k \int_0^Q \frac{dq}{x^2} = k\lambda \int_a^{a+L} \frac{dx}{x^2}} \quad (3) \quad \leftarrow \text{(1 pt extra credit)}$$