

SOUND

- a) There is NO sound in vacuum; you need matter to propagate a sound wave.
 b) SOUND: Any mechanical wave whose frequency lies between 20Hz and 20,000Hz, that is, $20\text{Hz} \leq f \leq 20\text{kHz}$ (It is called SOUND b/c you can hear it!)
 c) We will work with sound in Gases only-then sound is a purely Longitudinal wave.
 d) Sound is a longitudinal displacement wave or a longitudinal pressure wave.
 e) Periodic Sound wave *properties*

<u>DISPLACEMENT</u>	<u>PRESSURE</u>
<p>Sine wave, $\phi = 0$</p> $S = S_m \sin(kx - \omega t)$ <p>amplitude $S_m \parallel \hat{x}$</p> $\omega = vk$	<p>To write corresponding pressure wave we have to realize that the variation occurs so rapidly that there is no possibility for exchange of heat (DQ) to ensure equilibrium with surroundings, so $DQ=0$, sound is an <u>adiabatic process</u>: <i>Pressure and volume satisfy:</i></p> $P_0 V_0^\gamma = \text{constant.}$ <p>P_0 = ambient pressure</p> $\gamma = \frac{C_p}{C_v}, C_p = \text{sp ht at const } P$ $C_v = \text{sp ht at const } V$ $\gamma_{\text{monoatomic}} = \frac{5}{3}$ $\gamma_{\text{diatomic}} = \frac{7}{5}$ $\rightarrow \phi = \frac{-\pi}{2}$ $P = P_0 - \gamma P_0 S_m k \cos(kx - \omega t)$
<p>Displacement oscillates about zero.</p>	<p>Pressure oscillates about P_0</p> <p>Amp of pressure wave</p> $P_m = \gamma P_0 S_m k$ $P_m \parallel \hat{x}$ <p><i>Pressure is $\frac{\pi}{2}$ out of phase with displacement. where S is max, $(P-P_0) = 0!$</i></p>

f) Speed of sound in a gas

$$v = \sqrt{\frac{\gamma P_0}{\rho_0}} \quad \rho_0 = \text{ambient density}$$

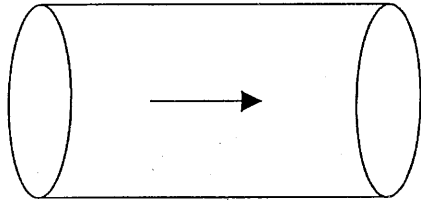
since $P_0 V_0 = N k_B T$ $[k_B = 1.383 \times 10^{-23} \text{ J/K}]$

If gas particles have mass m , we can write

$$P_0 = \frac{Nm}{V_0} \frac{k_B T}{m}, \text{ or } \frac{P_0}{\rho_0} = \frac{k_B T}{m}$$

$$v = \sqrt{\frac{\gamma k_B T}{m}} = \sqrt{\gamma} \frac{v_{rms}}{\sqrt{3}} \quad [T \text{ in Kelvin Scale}]$$

g) Intensity of sound wave: Imagine that the wave is traveling with velocity v through a tube of cross-section A .



Since $S = S_m \sin(kx - \omega t)$ the particle velocity is $V_p = S_m \omega \cos(kx - \omega t)$ and kinetic energy

per unit volume is $K \cdot E = \frac{1}{2} \rho_0 S_m^2 \omega^2$.

Volume of wave traveling past every cross-section will be Av in one second. Energy transport per second through area

$$A = \frac{1}{2} A \rho_0 S_m^2 \omega^2 v$$

Intensity $I =$ energy transport per second per m^2

$$= \frac{1}{2} \rho_0 S_m^2 \omega^2 v \quad \left[\rho_0 = \frac{\gamma P_0}{v^2} \right]$$

$$= \frac{1}{2} \gamma P_0 S_m^2 \frac{\omega^2}{v}$$

Please compare this with energy transport per second on wire $\langle P \rangle = \frac{1}{2} A^2 \frac{\omega^2}{v} F$

h) Smallest discernable intensity is $I_0 = 10^{-12} \text{ Watt/m}^2$

So we define decibels $db = 10 \log \frac{I}{I_0}$

[bel comes from Alexander Graham Bell]

That is $90db$ sound has $9 = \log \frac{I}{10^{-12}}$, $I = 10^{-3} \text{ Watt/m}^2$

i) Amplitude of displacement wave for I_0 ($\omega = 10^3 \text{ rad/s}$, $\gamma = 1.4$, $P_0 = 10^5 \text{ N/m}^2$),

$$10^{-12} = \frac{1}{2} \times 1.4 \times 10^5 \times \frac{S_m^2 \times 10^6}{340}$$

$$S_m \cong 10^{-10} \text{ m}$$

Roughly equal to diameter of hydrogen atom. REMARKABLE!!!

That is your Ear is sensitive to motion of air molecules whose displacement is ~~also~~ equal to the diameter of a Hydrogen Atom. Congratulations!!

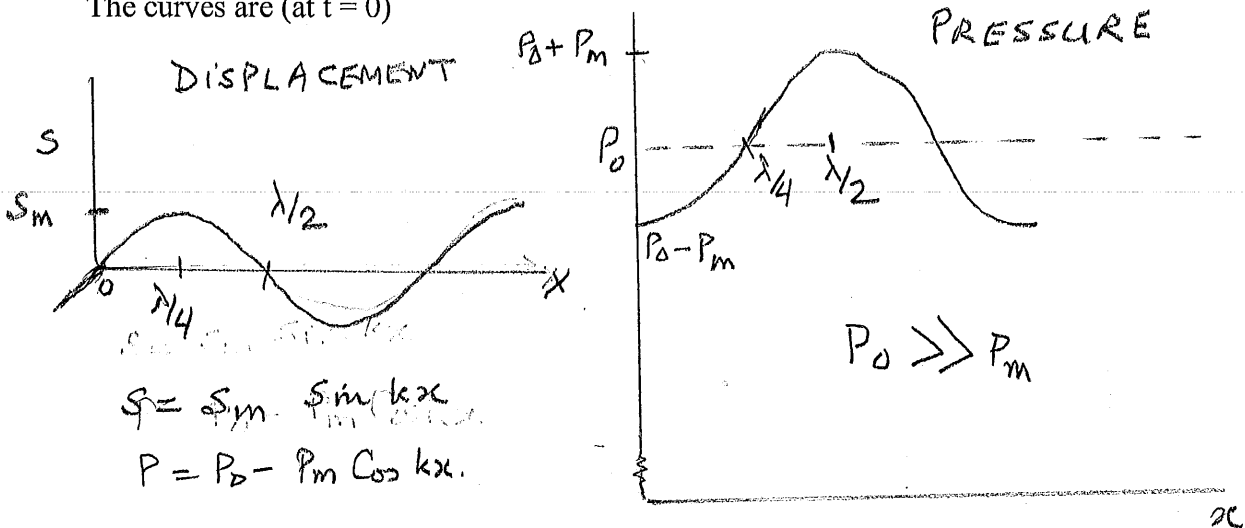
Special Note

Detailed interpretation of displacement and pressure curves in a sound wave

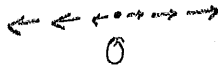
Or

Why is pressure variation $\pi/2$ out of phase with displacement as a function of position?

The curves are (at $t = 0$)



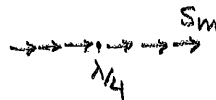
Near $x = 0$, displacements look like



All displacements away from 0.

That is displacements of particles increase rapidly as you go away from $x = 0$. Consequently, gas is in expansion. That is why pressure is at a minimum.

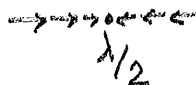
Near $x = \lambda/4$, displacements look like



That is, all the displacements are nearly equal so there is little change in volume and hence P is at its equilibrium value. Derivation from $\frac{dv}{dx}$ is zero. ~~near $x = \lambda/2$~~

NEAR $x = \lambda/2$

Displacements look like



Displacements are toward $\lambda/2$ and increase as you go away from $\lambda/2$. So here gas is in contraction and that is why pressure is at a maximum.

Crucial point is that change of volume and hence change of pressure happens only if displacement everywhere is not the same.