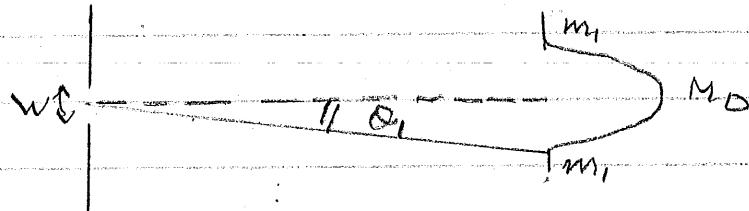


GEOMETRICAL OPTICS

BASIS: We have learnt that when light of wavelength λ passes through a slit of width w it spreads by the angle θ_1 given by

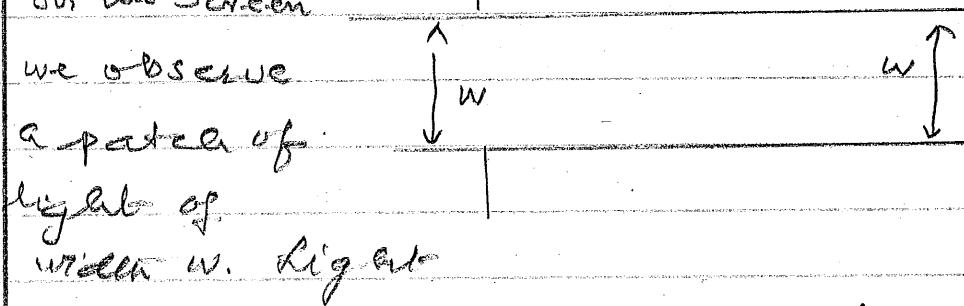
$$\sin \theta_1 = \frac{\lambda}{w}$$



If w becomes much larger than λ , $\theta_1 \rightarrow 0$ and this spread due to diffraction becomes negligible.

In that case the propagation of light looks like

and on the Screen

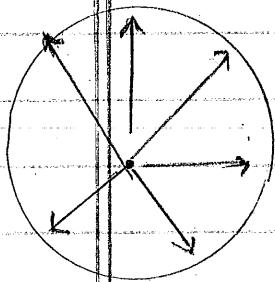


appears to be propagating along a straight line and therefore its progress can be described by using geometry, hence Geometrical optics

and we talk of the path of light by labelling a light RAY.

So far now we say that if openings and obstacles are much larger than λ , Geometrical optics prevails.

Even if one considers a point source where light would emerge radially, near the source the spheres are small



but far away they begin to look like "planes" and the light "rays" essentially become parallel to one another.



The basic principle which governs the propagation of light in Geometrical optics is due to Fermat

→ Fermat's principle: LIGHT INVARIABLY CHOOSES A PATH WHICH TAKES THE LEAST TIME OF TRAVEL.

Unobstructed light therefore travels in straight lines.

Next, we know that speed of light is not the same in all media. Indeed

$$v = \frac{c}{n} \quad (c = \text{speed in vacuum})$$

where n 's are refractive index.

Previously, we learnt that when a wave arrives at a point where velocity changes it gives rise to two waves - reflected wave travels back in original medium. Transmitted wave travels forward in next medium.

Light waves will do exactly the same

$\{$ reflection
refraction } reflected

Surface of separation →

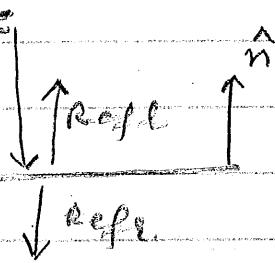
action

$\} n'$

Transmitted

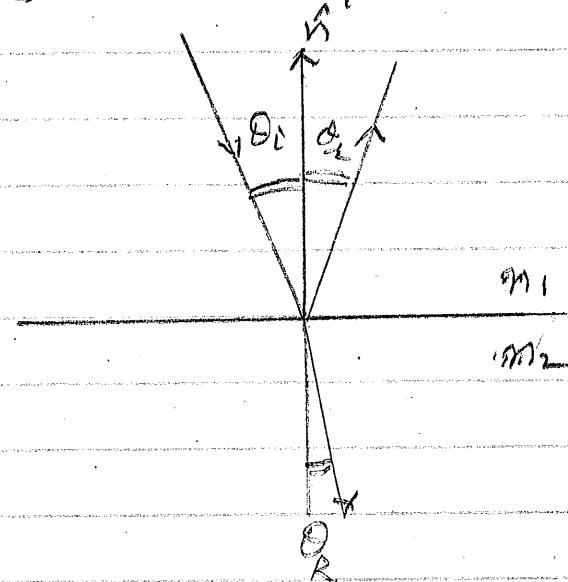
For light this is called "Refracted"

In ray picture if
light is travelling
along perpendicular
to surface you get →



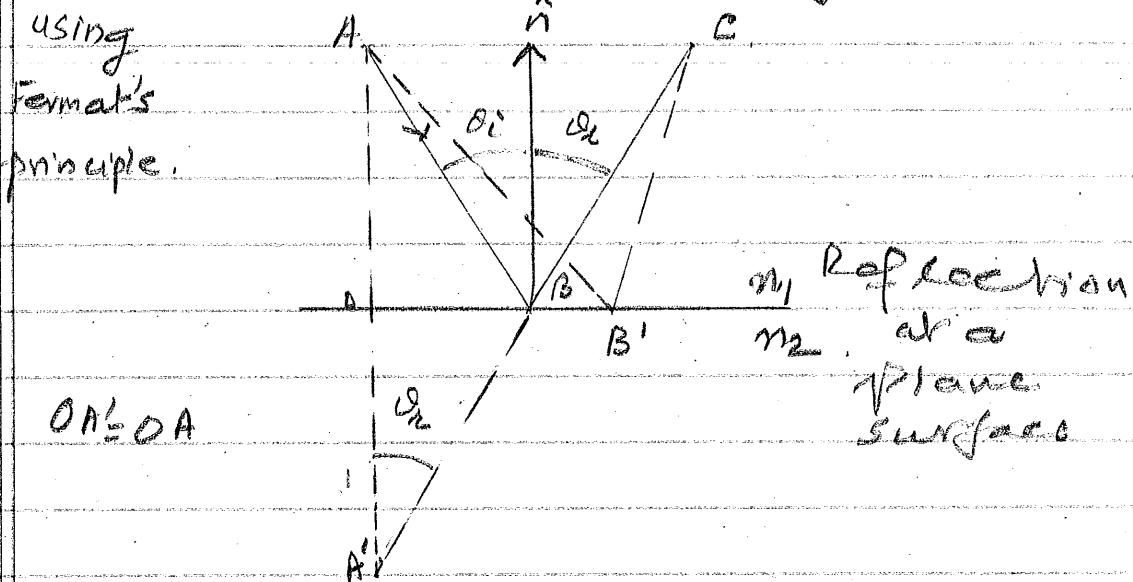
However, we are now interested in the
more general case where path of light is
not along \hat{n} the vector normal to the
surface.

NOTE Henceforward, all angles are to be
measured with respect to the NORMAL (\hat{n})



so now light is arriving at angle θ_2 . Fermat's principle controls the angles θ_2 (reflected ray) and θ_1 (refracted ray).

The reflection case is easy to understand using Fermat's principle.

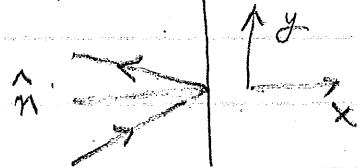


Notice that $A'B'C$ is the shortest distance light will travel going from A to C . All other paths are longer and therefore will take more time.

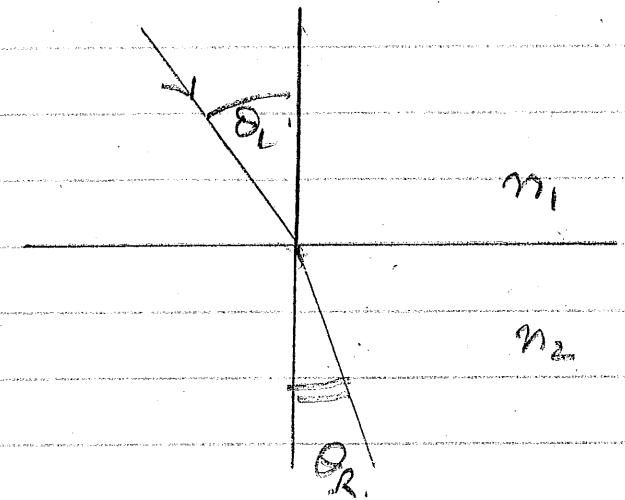
Hence we have Law of Reflection
Angle of reflection = angle of incidence

$$\boxed{\theta_2 = \theta_1}$$

[Looks like in case of Elastic Collision with a wall which we analyzed earlier 121, x-component of \vec{P} reversed. Y-component stayed the same]



The path of the refracted ray is also determined by Fermat's principle but the proof requires use of derivatives (which is a bonus for 122) so we just write the answer called SNELL'S LAW.



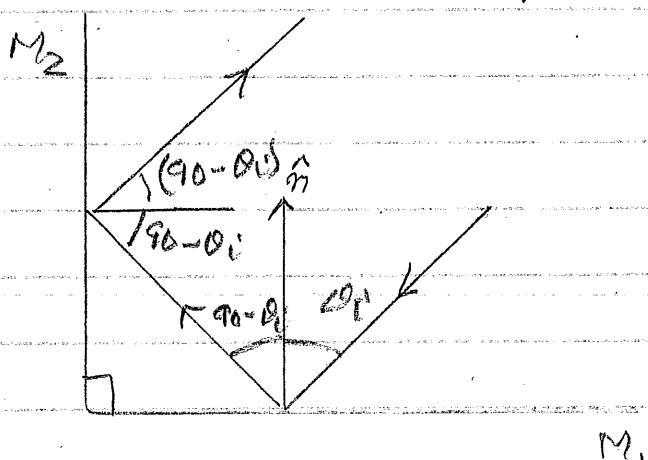
$$[n_2 \sin \theta_r = n_1 \sin \theta_i] \quad \text{Refraction}$$

Product of refractive index and sine of the angle w.r.t respect to normal is a constant.

SOME Applications

"CORNER" REFLECTOR - uses two mirrors, the mirror being a device where only reflections occur - a polished piece of metal, glass with silver coating.

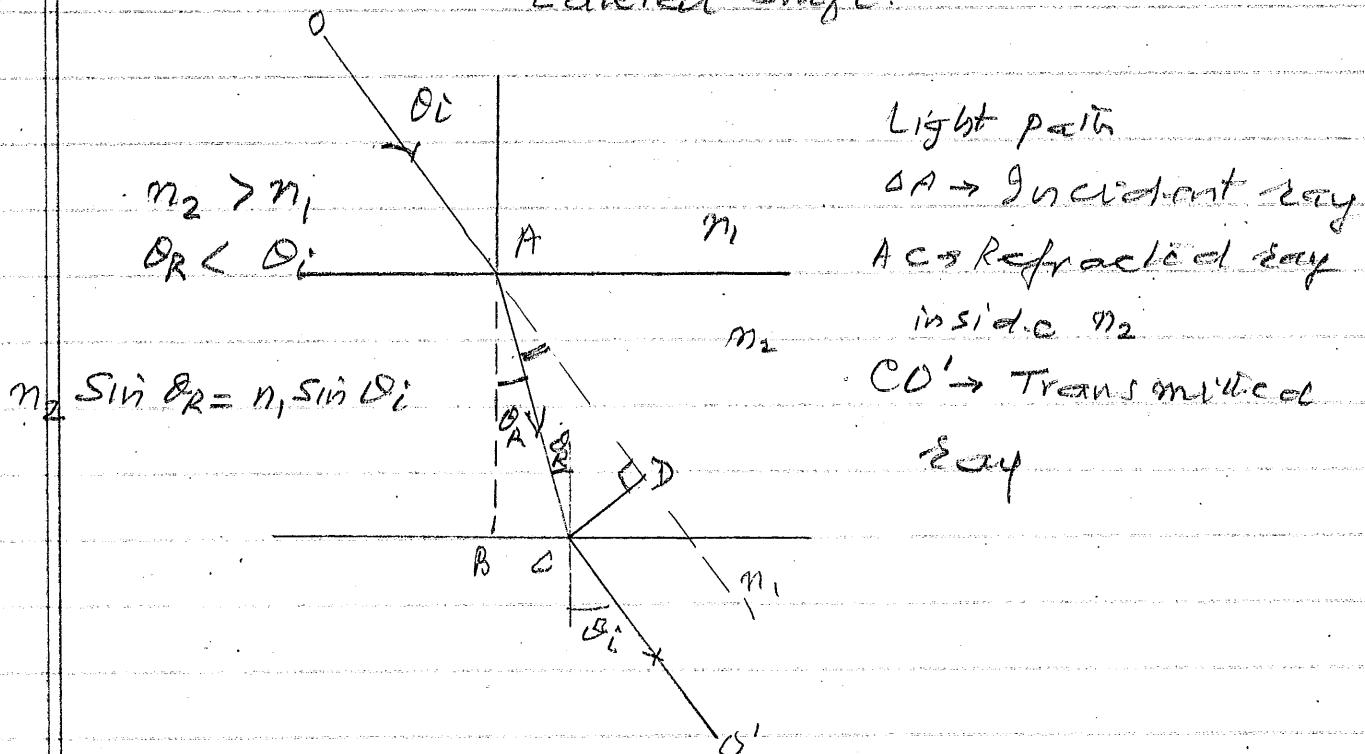
Two mirrors at right angles to one another



And from the figure above you can see
that after the two reflections we light
follows a path which is anti-parallel to
the incident ray.

Refraction Through parallel plate

- Lateral shift.



Notice that CO' is parallel to OA so the
light is shifted laterally by the amount CD .

In $\triangle ACD$, angle $CAD = (\theta_i - \theta_R)$

hence

$$\frac{CD}{AC} = \sin(\theta_i - \theta_R)$$

In $\triangle ABC$ $AB = t$ [thickness of slab]

$$\frac{t}{AC} = \cos \theta_R$$

hence $CD = \frac{t}{\cos \theta_R} [\sin \theta_i \cos \theta_R - \cos \theta_i \sin \theta_R]$

$$= t \sin \theta_i \left[1 - \frac{\cos \theta_i}{\sin \theta_i} \frac{\sin \theta_R}{\cos \theta_R} \right]$$

$$= t \sin \theta_i \left[1 - \frac{n_1}{n_2} \frac{\cos \theta_i}{\cos \theta_R} \right]$$

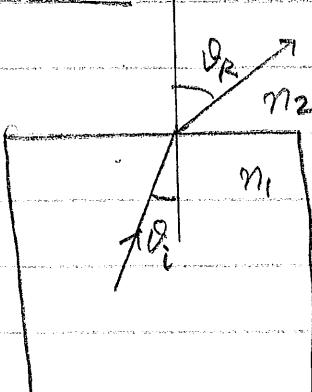
We will use this equation when we get to discussion of thin lenses.

Total Internal Reflection

Now $n_2 < n_1$

$$\text{Since } n_2 \sin \theta_R = n_1 \sin \theta_i$$

$$\theta_R > \theta_i$$



If you increase θ_i ,

θ_R increases until you

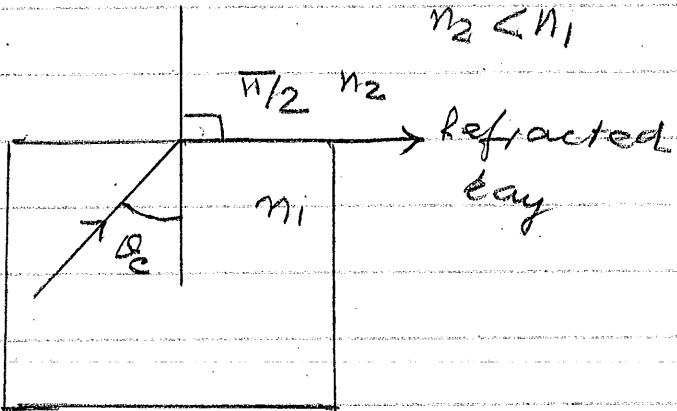
get the critical

case when refracted ray becomes parallel to the surface.

Now $\theta_R = \frac{\pi}{2}$

$$n_2 \sin \frac{\pi}{2} = n_1 \sin \theta_c$$

$$\sin \theta_c = \frac{n_2}{n_1}$$

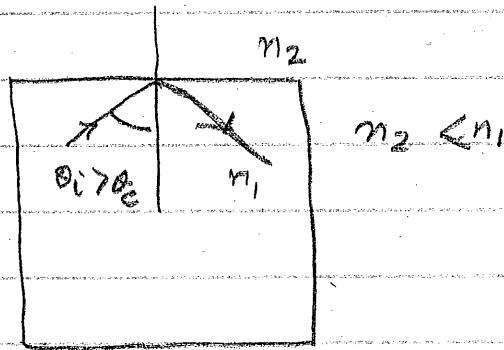


Example Glass $n_1 = 1.5$

Air $n_2 = 1$ $\sin \theta_c = \frac{1}{1.5}$

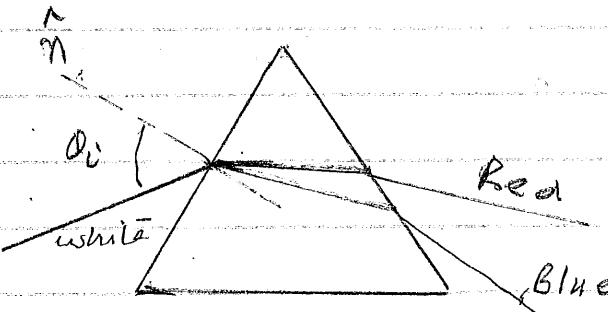
$$\theta_c \approx 41^\circ$$

If you make θ_i larger than θ_c no light can go out — Total Internal Reflection



Newton's Experiments

He passed white light through a prism and found that it split into many colored rays.



Technically we say light is dispersed into its Component colors hence Dispersion.

What did we learn?

① In vacuum speed of light is same for all colors

② White light is a composite of many colors V → I → B → G → Y → O → R.

 Violet Indigo Blue Green Yellow Orange Red

(Now we know λ's in vac go from 400nm to 700nm)

③ Speed of light in a medium is NOT THE SAME FOR ALL COLORS, that's why they split.

④ $\text{Red} > \text{Blue}$, but both satisfy Snell's law

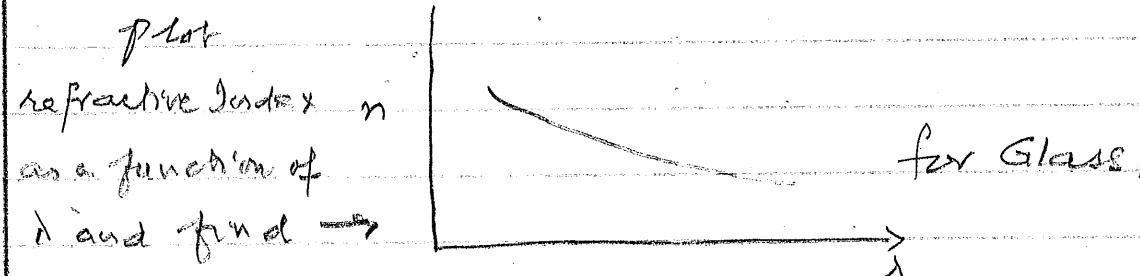
$$n_{\text{Red}} \sin \theta_{\text{Red}} = n_{\text{Blue}} \sin \theta_{\text{Blue}}$$

$$\text{so } n_{\text{Red}} < n_{\text{Blue}}$$

$$\frac{c}{v_{\text{Red}}} < \frac{c}{v_{\text{Blue}}}$$

$$v_{\text{Red}} > v_{\text{Blue}}$$

⑤ Now that we know the wavelengths we can



⑥ Our perception of color is controlled by frequency and not wavelength.