

BCs, e.g. $E_{\parallel}^1 = E_{\parallel}^2$:

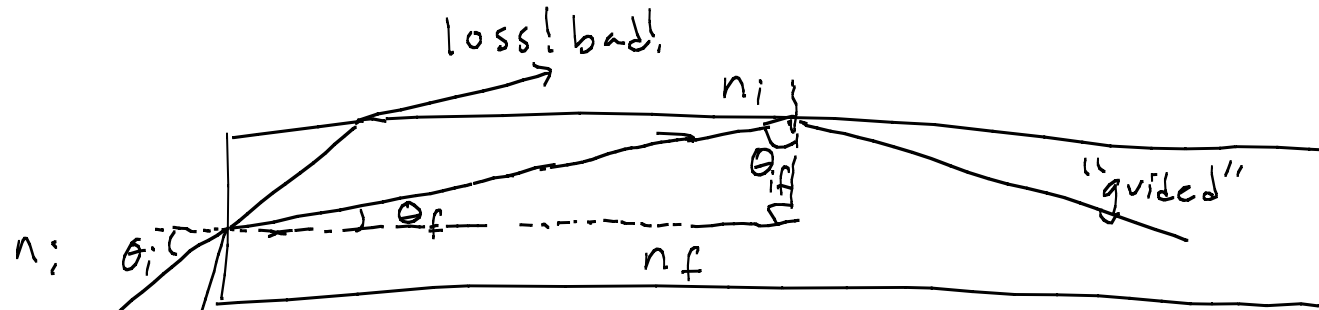
$$\cos \theta_i e^{ik_1(\cos \theta_i z + \sin \theta_i x)} \Big|_{z=0} + r \cos \theta_r e^{ik_1(-\cos \theta_r z + \sin \theta_r x)} \Big|_{z=0} = t \cos \theta_t e^{ik_2(\cos \theta_t z + \sin \theta_t x)} \Big|_{z=0}$$

This is only true for all x if:

$$k_1 \sin \theta_i = k_1 \sin \theta_r = k_2 \sin \theta_t \quad \frac{\omega}{k_1} = \frac{c}{n_1} \quad k_1 = \frac{n_1 \omega}{c}$$

$$\theta_i = \theta_r \quad n_1 \sin \theta_i = n_2 \sin \theta_t$$

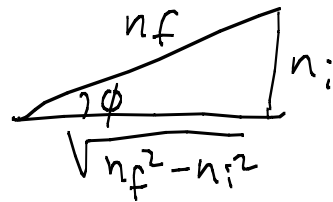
TIR application: fiber optics



top surface: (sides of fiber) $n_f \sin \theta_{if}^c = n_i \sin \frac{\pi}{2} \rightarrow \theta_{if} > \theta_{if}^c = \sin^{-1} \frac{n_i}{n_f}$

$$\sin \theta_f = \cos \theta_{if}$$

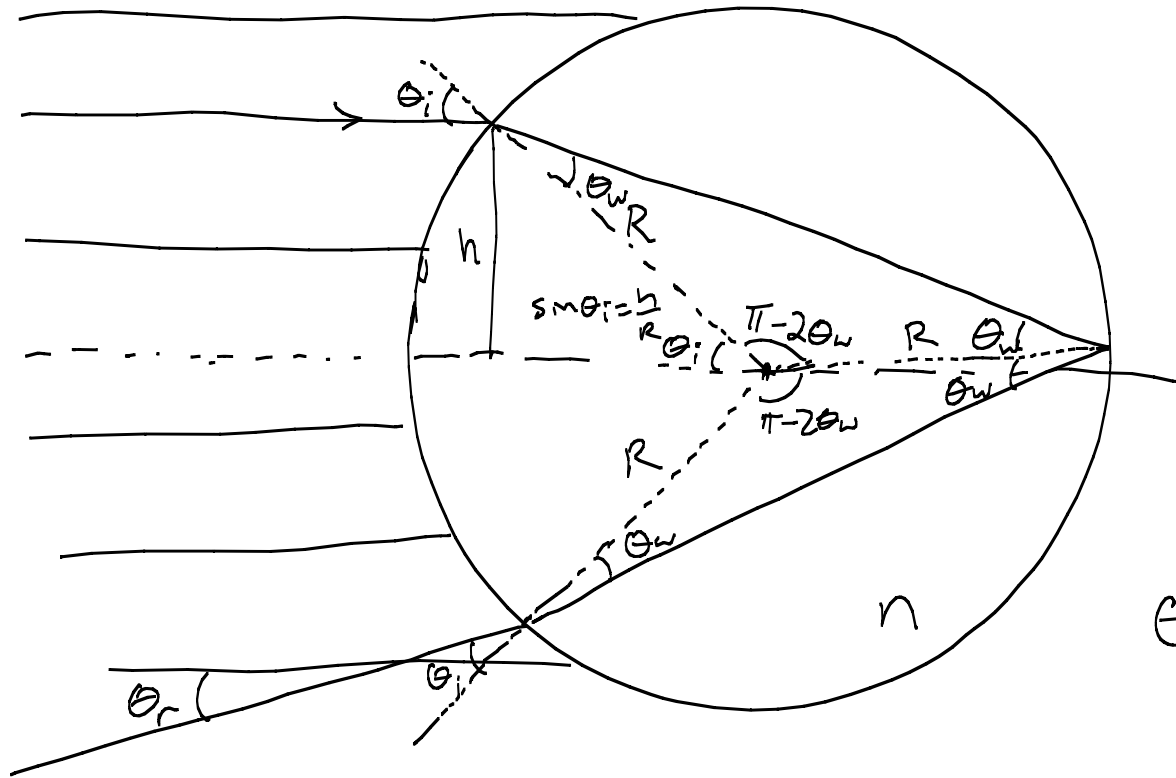
Input interface: $n_i \sin \theta_i^c = n_f \sin \theta_f^c = n_f \cos \theta_{if}^c = n_f \cos(\sin^{-1} \frac{n_i}{n_f})$



$$n_i \sin \theta_i^c = n_f \frac{\sqrt{n_f^2 - n_i^2}}{n_f}$$

$$\theta_i < \theta_i^c = \sin^{-1} \frac{\sqrt{n_f^2 - n_i^2}}{n_i} = \sin^{-1} \sqrt{\left(\frac{n_f}{n_i}\right)^2 - 1}$$

Refraction and Reflection in a sphere



$$\theta_{tot} = 2(\pi - 2\theta_w) + 2\theta_i$$

$$\theta_r = 2\pi - \theta_{tot} = 4\theta_w - 2\theta_i$$

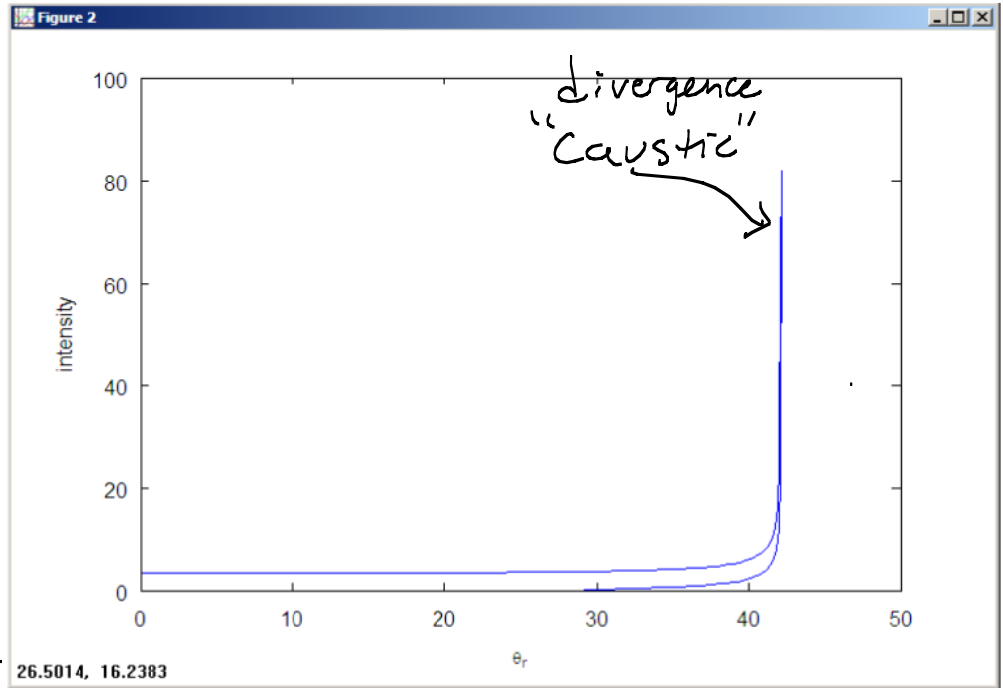
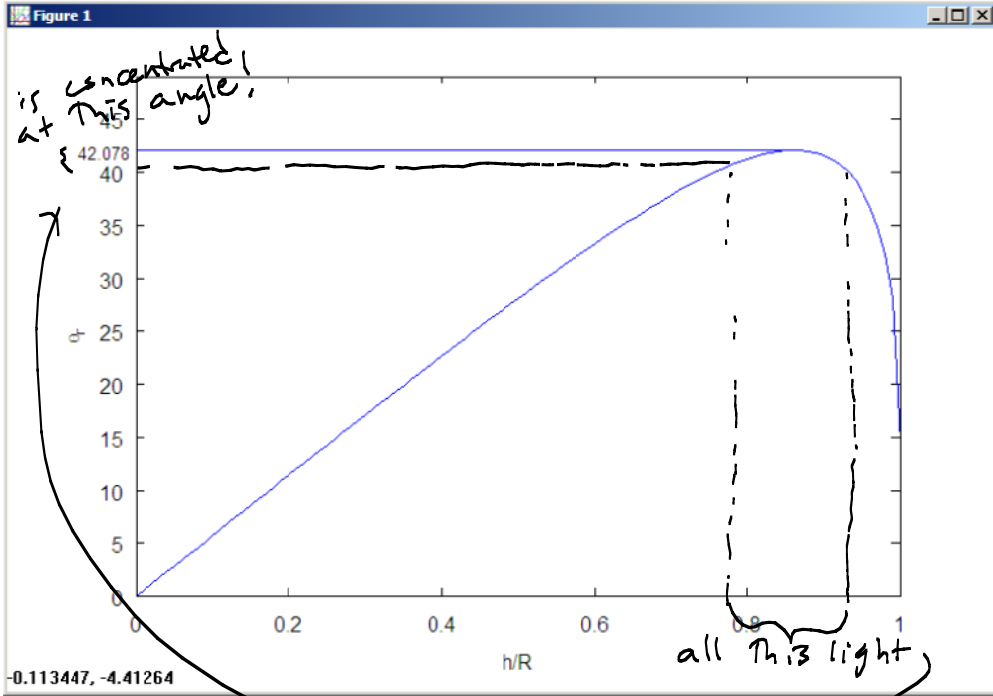
$$= 4 \sin^{-1} \left(\frac{\sin \theta_i}{n} \right) - 2\theta_i$$

$$\theta_i = \sin^{-1} \frac{h}{R}$$

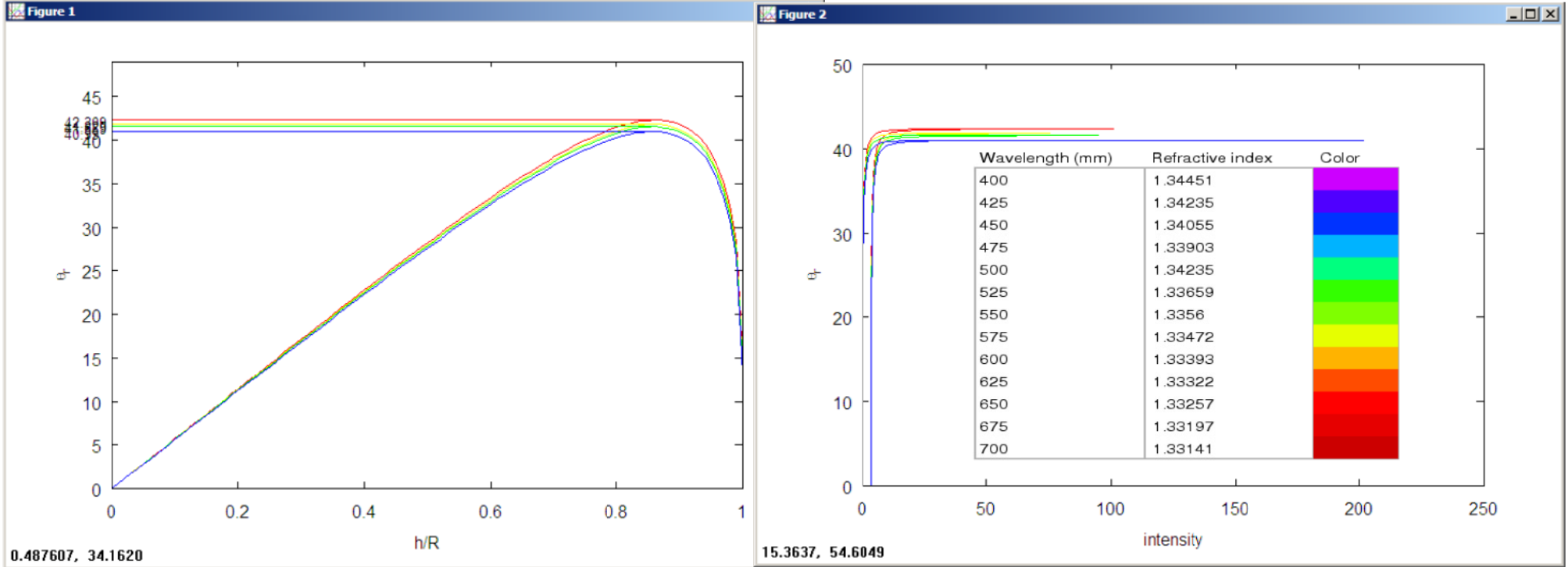
$$\sin \theta_i = n \sin \theta_w$$

$$\theta_w = \sin^{-1} \frac{\sin \theta_i}{n}$$

Caustics



Rainbows



← Second rainbow from 2 internal reflections
 → colors reversed!
 ← primary rainbow